

1 **Complex conductivity tensor of anisotropic hydrocarbon-**  
2 **bearing shales and mudrocks**

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16 **Short title:** Complex conductivity anisotropy

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24 *Intended for publication in Geophysics*

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26 **Abstract.** A model was recently introduced to describe the complex electrical conductivity  
27 and high frequency dielectric constant of isotropic clayey porous materials. That approach is  
28 generalized here to the case of anisotropic and tight hydrocarbon-bearing shales and  
29 mudrocks by introducing tensorial versions of both formation factor and tortuosity. It is  
30 shown that in-phase and quadrature conductivity tensors have common eigenvectors, but that  
31 the eigenvectors of the dielectric tensor may be different due to influence of the solid phase at  
32 high frequencies. In-phase and quadrature contributions to complex electrical conductivity  
33 depend on saturation, salinity, porosity, temperature, and cation exchange capacity  
34 (alternatively, specific surface area) of the porous material. Kerogen is likely to have a  
35 negligible contribution to the cation exchange capacity of the material because all  
36 exchangeable sites in the functional groups of organic matter may have been polymerized  
37 during diagenesis. An anisotropic experiment is performed to validate some of the properties  
38 described by the proposed model, especially to verify that the electrical anisotropy factor is  
39 the same for both in-phase and quadrature conductivities. We use two samples from the  
40 Bakken formation. Experimental data confirm the validity of the model. It is also found that  
41 the range of values for cation exchange capacity determined when implementing the new  
42 model with experimental data agree with the known range of cation exchange capacity for the  
43 Bakken shale. Measurements indicate that the bulk-space tortuosity in the direction normal to  
44 bedding plane can be higher than 100.

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## INTRODUCTION

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Shale formations are of increasing interest in hydrocarbon exploration worldwide. They comprise a diverse set of rock types, but are generally characterized as fine-grained, low porosity and low permeability rocks, with a non-negligible clay fraction in terms of bulk petrophysical properties. Due to preferential orientation of mineral foliations and finely laminated bedding planes, shales and mudrocks are almost ubiquitously anisotropic in several of their macroscopic physical properties. The term mudrock is used to describe all fine grained shaly and non-shaly formations. It is of great interest to petrophysicists to develop new models to describe seismic and electromagnetic (EM) measurements in these anisotropic materials.

Oil-shale deposits correspond to immature, organic-rich source rocks resulting in high kerogen mass fractions due to limited burial and thermal maturation histories—effectively, they have not been heated sufficiently to release their hydrocarbons. Hence, oil shales and mudrocks are typically water-wet, single- or dual-phase fluid systems, characterized by a heterogeneous solid phase comprising both siliciclastic, carbonate, and organic components. Mudrock-oil formations involve complex multiphase fluid systems, in which the degradation of kerogen, through geochemical thermal maturation processes (i.e., catagenesis and metagenesis), has both altered the nature of the solid fraction and produced economically significant polar and non-polar, aromatic and hydrocarbon fluid fractions. Oil-shale and shale-oil deposits represent two generalized regimes in the continuum of shale thermal maturation, exhibiting measurable differences in the characteristics of both solid and fluid phases. In what follows, we refer to all these rock formations in a general manner as shales, tacitly implying that their properties are intrinsically related to the maturation history of each formation. Note however, that mudrocks is a geologically more appropriate term to use since that term denotes does not specify any lithology, rather it denotes a fine-grained rock system.

71           There is a growing need to better characterize the so-called “sweet spots” of tight oil-  
72 mudrock formations using an arsenal of geophysical methods with the objective to optimize  
73 hydrocarbon detection and production. Among such methods, galvanic and EM measurements  
74 can be used to determine the complex electrical conductivity of formations through borehole  
75 and cross-well imaging. What is missing is a general effective complex electrical  
76 conductivity model specific for shales and mudrocks, which includes the relative effects of  
77 porosity, water saturation, kerogen content and type, clay content and type, and a tortuosity  
78 tensor describing the anisotropy of the material (generally expected to be transversely  
79 isotropic, TI). As discussed in Revil (2013), such a model should also include the description  
80 of the high frequency permittivity of the material and possibly Maxwell-Wagner polarization.  
81 Recent developments in logging technology now allow one to resolve the macroscopic effects  
82 of anisotropy. Despite progresses on the experimental front (e.g., Weller et al., 2010), robust  
83 theoretical models describing the full effective complex conductivity tensor are still lacking  
84 (Bittar et al., 2009).

85           Revil and colleagues (Leroy et al., 2008; Leroy and Revil, 2009; Revil and Florsch,  
86 2010) have recently invoked a strong role of the Stern layer (the inner portion of the electrical  
87 double layer coating the surface of mineral grains) to explain the low-frequency polarization  
88 of mixed, sandy, and clayey materials. The model of Stern layer polarization appears to be  
89 reliable to explain the dependence of complex electrical conductivity on cation exchange  
90 capacity (CEC) and specific surface area (Revil, 2012, 2013), salinity (Revil and Skold, 2011;  
91 Weller and Slater, 2012), pH (Skold et al., 2011), sorption of cations and organic molecules  
92 (Vaudelet et al., 2011a, b; Schwartz and Furman, 2012), influence of grain size (Revil et al.,  
93 2012), the relationship between surface conductivity and quadrature conductivity (Revil and  
94 Florsch, 2010; Revil, 2012), temperature (Zisser et al., 2010a), and water saturation (Revil et  
95 al., 2012; Revil, 2013). Here, we generalize this model to the case of anisotropic formations

106 with the intent to quantify the role played by kerogen on both surface conductivity and  
 107 quadrature conductivity. Beside the contribution of the electrical double layer of non-  
 108 conducting minerals, there is also a strong role played by the presence of pyrite above oil  
 109 reservoirs (e.g., Veeken et al., 2009) and in the shallow subsurface associated with the  
 110 biochemistry of contaminant plumes (Flores Orozco et al., 2011). Pyrite plays an active role  
 111 in spectral induced polarization as long as its surface has not been oxidized. In addition, with  
 112 the exception of the work by Zisser and Nover (2009) and Zisser et al. (2010b), there are a  
 113 few open publications documenting and or explaining the polarization and anisotropy of tight  
 114 (low-permeability) porous rocks.

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## 106 THE ISOTROPIC CASE AND ITS GENERALIZATION

### 107 Ampère's law in isotropic media

108 Let  $\omega = 2\pi f$  designate angular frequency and  $f = \omega / (2\pi)$  linear frequency (in Hertz).

109 For isotropic materials, Ampère's law is written as (e.g., Vinegar and Waxman, 1984)

$$110 \quad \nabla \times \mathbf{H} = [\sigma_{eff} - i\omega\epsilon_{eff}] \mathbf{E}, \quad (1)$$

$$111 \quad \sigma_{eff} = \sigma'(\omega) + \omega\epsilon''(\omega), \quad (2)$$

112 and

$$113 \quad \epsilon_{eff} = \epsilon'(\omega) - \frac{\sigma''(\omega)}{\omega}, \quad (3)$$

114 where  $\mathbf{H}$  and  $\mathbf{E}$  denote magnetic and electrical fields, respectively,  $i = \sqrt{-1}$  denotes the pure  
 115 imaginary number, and  $\sigma'$  and  $\sigma''$  (expressed in  $\text{S m}^{-1}$ ) denote the real (in-phase) and  
 116 imaginary (out-of-phase or quadrature) components of the complex conductivity  $\sigma^*$ ,  
 117 respectively, and are given by

$$118 \quad \sigma^* = \sigma' + i\sigma'' = |\sigma| \exp(i\varphi), \quad (4)$$

119 with the magnitude of the conductivity written as  $|\sigma^*| = (\sigma'^2 + \sigma''^2)^{1/2}$  and the phase lag,  $\varphi$ ,  
 120 given by  $\tan \varphi = \sigma'' / \sigma'$ . In the frequency range 0.1 - 1000 Hz, in-phase and quadrature  
 121 conductivities are only slightly frequency dependent because grain polarization occurs over a  
 122 broad range of scales (Vinegar and Waxman, 1984; Revil, 2012, 2013). Complex  
 123 conductivity is written as  $\varepsilon^* = \varepsilon' + i\varepsilon''$ . By neglecting the polarization of water molecules  
 124 (above 1 GHz) and Maxwell Wagner polarization, one can safely neglect the imaginary  
 125 component of the dielectric constant, whereby  $\varepsilon^* \approx \varepsilon'$ , thus giving rise to the approximation  
 126  $\sigma_{eff} \approx \sigma'(\omega)$ .

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### 128 **In-phase conductivity**

129 Revil (2013) developed a new model to describe the complex conductivity of clayey  
 130 materials using a volume-average approach. According to Revil (2013) and assuming  
 131 volumetric averaging to describe effective conductivity, the in-phase conductivity  $\sigma'$  (in S m<sup>-1</sup>)  
 132 of porous materials is given as a function of pore water conductivity  $\sigma_w$  (in S m<sup>-1</sup>) by the  
 133 expression

$$134 \quad \sigma' = \frac{1}{F} \left\{ S_w^n \sigma_w + S_w^p \left( \frac{F-1}{F\phi} \right) \rho_s [\beta_{(+)}(1-f) + \beta_{(+)}^s f] \text{CEC} \right\}, \quad (5)$$

135 where  $F$  (dimensionless) denotes the (intrinsic) formation factor for resistivity. It is related to  
 136 connected porosity  $\phi$  by Archie's equation  $F = \phi^{-m}$  where  $m$  (dimensionless) denotes the  
 137 porosity exponent. The total connected porosity entering Archie's law does not distinguish  
 138 between kerogen and matrix porosities. The parameters  $n$  and  $p$  (both dimensionless) denote  
 139 the second Archie exponent (saturation exponent) and the saturation exponent for surface  
 140 conductivity, respectively (with  $p=n-1$  as introduced by Vinegar and Waxman, 1984 and  
 141 demonstrated by Revil, 2013, using a volume-averaging approach),  $f$  denotes the fraction of  
 142 counterions in the Stern layer (see Leroy et al., 2008 and Revil, 2012, for discussion for sand

143 and clayey materials),  $\rho_s$  denotes mass density of the solid phase (typically  $2650 \pm 50 \text{ kg m}^{-3}$   
 144 for the crystalline framework of clay minerals),  $\beta_{(+)}$  is the mobility of counterions in the  
 145 diffuse layer, and  $\beta_{(+)}^S$  is the mobility of counterions in the Stern layer (both in  $\text{m}^2\text{s}^{-1}\text{V}^{-1}$ ). For  
 146 clay minerals, the mobility of counterions in the diffuse layer is equal to the mobility of the  
 147 same counterions in bulk pore water (e.g.,  $\beta_{(+)}(\text{Na}^+, 25^\circ\text{C}) = 5.2 \times 10^{-8} \text{ m}^2\text{s}^{-1}\text{V}^{-1}$ , see Revil,  
 148 2012). Mobility of counterions in the Stern layer is substantially smaller and equal to  
 149  $\beta_{(+)}^S(25^\circ\text{C}, \text{Na}^+) = 1.5 \times 10^{-10} \text{ m}^2\text{s}^{-1}\text{V}^{-1}$  for clay minerals (Revil, 2012, 2013). The acronym  
 150 CEC (expressed in  $\text{C kg}^{-1}$ ) denotes cation exchange capacity of the material. In equation 5,  $S_w$   
 151 denotes saturation of the water phase ( $S_w = 1$  for a water-saturated material).

152 Because the formation factor is generally much higher than unity for tight formations  
 153 ( $F \gg 1$ ), equation 5 can be written as

$$154 \quad \sigma' \approx \frac{1}{F} S_w^n \sigma_w + S_w^p \left( \frac{1}{F\phi} \right) \rho_s [\beta_{(+)}(1-f) + \beta_{(+)}^S f] \text{CEC}. \quad (6)$$

155 The second additive term in this last equation corresponds to the surface conductivity  $\sigma_s$ .  
 156 Equation 6 is also very close to the equation proposed by Revil et al. (1996) (their equation  
 157 15) for water-saturated doleritic core samples from the oceanic crust. A simple generalization  
 158 of the above expression to anisotropic media yields the following expression for the in-phase  
 159 conductivity tensor:

$$160 \quad \boldsymbol{\sigma}' = \sigma_{ij}' \mathbf{x}_i \otimes \mathbf{x}_j, \quad (7)$$

$$161 \quad \mathbf{F} = F_{ij} \mathbf{x}_i \otimes \mathbf{x}_j, \quad (8)$$

$$162 \quad \mathbf{T} = T_{ij} \mathbf{x}_i \otimes \mathbf{x}_j, \quad (9)$$

163 and

$$164 \quad \sigma_{ij}' \approx F_{ij} (S_w^n \sigma_w) + T_{ij} S_w^p \rho_s [\beta_{(+)}(1-f) + \beta_{(+)}^S f] \text{CEC}, \quad (10)$$

165 where  $\mathbf{x}_i$  ( $i = 1, 2, 3$ ) denote the basis vectors of the Cartesian frame of reference ( $\mathbf{x}_i \cdot \mathbf{x}_j = \delta_{ij}$   
 166 where  $\delta_{ij}$  denotes the Kronecker delta),  $\mathbf{a} \otimes \mathbf{b}$  represents the tensorial product between vectors  
 167  $\mathbf{a}$  and  $\mathbf{b}$ ,  $F_{ij}$  denotes the components of the (symmetric second-rank) formation factor tensor  
 168 for the conductivity  $\mathbf{F}$ , and  $T_{ij}$  denotes the components of the (symmetric second-rank)  
 169 tortuosity tensor of the pore space  $\mathbf{T}$ . We designate  $\mathbf{T}$  as a connectivity tensor, as its entries  
 170 vary between 0 and 1 and represent the inverse of the tortuosity defined in the isotropic case  
 171 (see Bear, 1988; Bear and Bachmat, 1991; Bear and Cheng, 2010). Usually, in clayey  
 172 materials, one has  $\beta_{(+)}(1-f) \gg \beta_{(+)}^S f$  (Revil, 2012, 2013) whereby the last term of equation  
 173 10 can be further simplified to  $T_{ij} S_w^p \rho_s \beta_{(+)}(1-f) \text{CEC}$ . Our model also assumes that the  
 174 saturation exponent remains more or less the same in different directions. We will see later  
 175 that this assumption agrees well with the experimental data.

176 The components of the conductivity formation tensor and connectivity tensor are  
 177 related to each other by

$$178 \quad F_{ij} = T_{ij} \phi. \quad (11)$$

179 Therefore, both conductivity formation factor and connectivity tensors share the same  
 180 eigenvectors and, for the case of TI materials, the anisotropy ratio should be the same for bulk  
 181 and surface conductivities. This important technical point will be experimentally verified in  
 182 the last section of the present paper. In the isotropic case, one has

$$183 \quad F_{ij} = (1/F) \delta_{ij}, \quad (12)$$

184 whereby

$$185 \quad T_{ij} = (1/F\phi) \delta_{ij}. \quad (13)$$

186 Note that the tortuosity,  $\tau$ , of the pore space in the isotropic case ( $\tau \geq 1$ ) is defined as (e.g.,  
 187 Pride, 1994; Zhang and Knackstedt, 1995; Clennell, 1997; Sevostianova et al., 2010; Zhang  
 188 and Sherer, 2012)

$$189 \quad F = \frac{\tau}{\phi}, \quad (14)$$



190 
$$\tau = F\phi = \phi^{1-m}, \quad (15)$$

191 where we have used Archie's equation ( $F = \phi^{-m}$  with  $m$  designating the porosity exponent,  
 192 Archie, 1942). The iso-conductivity point designates the point characterized by a  
 193 macroscopic conductivity equal to the pore water conductivity (e.g., Revil et al., 1998).  
 194 Above the iso-conductivity point, surface and quadrature conductivity share the same bulk  
 195 tortuosity, as discussed, for instance, by Revil and Glover (1997); the reason is the following:  
 196 above the iso-conductivity point, surface conductivity is only a perturbation to the pore water  
 197 conductivity and the electrical field is controlled by the conductivity of the pore space (see  
 198 discussion in Bernabé and Revil, 1995, and Revil and Glover, 1997). Such a behavior  
 199 explains why the same tortuosity is applied to the bulk and surface conductivities in the "high-  
 200 salinity" regime. When surface conductivity dominates, conductivity is controlled by the  
 201 distribution of surface conductance, and the tortuosity of electrical current along the surface  
 202 of the minerals is different (usually higher) from that in pore water (see Bernabé and Revil,  
 203 1995, for a pore network modeling of this effect).

204

### 205 **Quadrature conductivity**

206 The expression for quadrature conductivity obtained by Revil (2013) is

207 
$$\sigma'' \approx S_w^p \left( \frac{1}{F\phi} \right) \rho_s \beta_{(+)}^s f \text{CEC}. \quad (16)$$

208 We emphasize that the explicit dependence of quadrature conductivity on the inverse of the  
 209 product ( $F\phi$ ) and on water saturation raised to the power  $p = n - 1$  are consistent with findings  
 210 by Vinegar and Waxman (1984) and Revil (2013). However equation 16 is based on a  
 211 volume averaging procedure while Vinegar and Waxman's (1984) model is predominantly  
 212 based on empirical considerations. Equation 16 agrees with Vinegar and Waxman's (1984)  
 213 observations in the laboratory (see also Revil, 2012 and 2013 for some tests using additional

214 data sets). Field observations also confirm an effect of oil saturation upon quadrature  
 215 conductivity (e.g., Olhoeft, 1986; Deceuster and Kaufmann, 2012).

216 The generalization of equation 16 to anisotropic media is straightforward, namely,

$$217 \quad \boldsymbol{\sigma}'' = \sigma_{ij}'' \mathbf{x}_i \otimes \mathbf{x}_j, \quad (17)$$

218 and

$$219 \quad \sigma_{ij}'' = T_{ij} S_w^p \rho_s \beta_{(+)}^S f_M \text{CEC}. \quad (18)$$

220 where  $\boldsymbol{\sigma}''$  denotes the complex conductivity tensor and  $\sigma_{ij}''$  identifies the entries of this  
 221 tensor. Our model also assumes that the  $p$ -exponent remains more or less the same in  
 222 different directions like for the saturation exponent. We will see later that this assumption  
 223 agrees well with the experimental data.

224 The complex conductivity tensor is defined as,

$$225 \quad \boldsymbol{\sigma}^* = \sigma_{ij}^* \mathbf{x}_i \otimes \mathbf{x}_j, \quad (19)$$

226 and

$$227 \quad \sigma_{ij}^* = \sigma_{ij}' + i\sigma_{ij}'', \quad (20)$$

228 where  $\sigma_{ij}'$  and  $\sigma_{ij}''$  are given by equations 10 and 18, respectively.

229

### 230 **Dielectric constant**

231 The remaining component of the generalized model is the (true or high-frequency)  
 232 dielectric constant of porous material. In what follows, the notation  $\varepsilon_w$  and  $\varepsilon_o$  designates the  
 233 dielectric constant of the water and oil phases, respectively, while  $\varepsilon_s$  designates the dielectric  
 234 constant of the solid phase. By invoking volume averaging, Revil (2013) obtained

$$235 \quad \varepsilon' = \frac{1}{F} \left[ S_w^n \varepsilon_w + (1 - S_w^n) \varepsilon_o + (F - 1) \varepsilon_s \right], \quad (21)$$

236 which can be simplified as

237 
$$\boldsymbol{\varepsilon}' = \frac{1}{F} \left[ S_w^n \boldsymbol{\varepsilon}_w + (1 - S_w^n) \boldsymbol{\varepsilon}_o \right] + \boldsymbol{\varepsilon}_s \quad (22)$$

238 for tight formations (recalling that  $F \gg 1$ ). For anisotropic formations, equation 22 can be  
239 generalized as

240 
$$\boldsymbol{\varepsilon} = \varepsilon_{ij} \mathbf{x}_i \otimes \mathbf{x}_j, \quad (23)$$

241 and

242 
$$\varepsilon_{ij} = F_{ij} \left[ S_w^n \boldsymbol{\varepsilon}_w + (1 - S_w^n) \boldsymbol{\varepsilon}_a \right] + \varepsilon_{ij}^s, \quad (24)$$

243 where  $\varepsilon_{ij}^s$  designates the components of the dielectric tensor of the solid phase

244  $\boldsymbol{\varepsilon}_s = \varepsilon_{ij}^s \mathbf{e}_i \otimes \mathbf{e}_j$ . Note that the eigenvectors of this tensor correspond to the anisotropy of the

245 solid matrix, and may be different from the eigenvectors associated with the tortuosity tensor

246 of the pore space. In tight formations, the entries of  $\boldsymbol{\varepsilon}_s$  can be obtained by taking the core

247 sample *in vacuo*, and measuring the components of the dielectric tensor in different

248 directions. That said, we expect that in most conditions the eigenvectors of the dielectric

249 constant to be aligned with the eigenvectors of the complex conductivity tensor. Josh et al.

250 (2012) observed that the anisotropy ratio can reach a factor 5 for the high frequency dielectric

251 constant ( $>0.1$  GHz).

252

### 253 **Ampère's law in anisotropic media**

254 The general form of Ampère's law in tight formations is, therefore, given by

255 
$$\nabla \times \mathbf{H} = \left[ \boldsymbol{\sigma}_{eff} - i\omega \boldsymbol{\varepsilon}_{eff} \right] \cdot \mathbf{E}, \quad (25)$$

256 
$$\boldsymbol{\varepsilon}_{eff} = \varepsilon_{ij}^{eff} \mathbf{x}_i \otimes \mathbf{x}_j, \quad (26)$$

257 
$$\boldsymbol{\sigma}_{eff} = \sigma_{ij}^{eff} \mathbf{x}_i \otimes \mathbf{x}_j, \quad (27)$$

258 
$$\sigma_{ij}^{eff} \approx \sigma_{ij}' \approx F_{ij} \left( S_w^n \sigma_w \right) + T_{ij} S_w^p \rho_s \beta_{(+)} (1 - f) \text{CEC}. \quad (28)$$

259 and

$$\varepsilon_{ij}^{eff} = F_{ij} [S_w^n \varepsilon_w + (1 - S_w^n) \varepsilon_a] + \varepsilon_{ij}^S - \frac{1}{\omega} T_{ij} S_w^p \rho_s \beta_{(+)}^S f_M \text{ CEC}. \quad (29)$$

261 The above equations neglect an important polarization mechanism in the intermediate  
 262 frequency range (0.1 MHz-100 MHz), often referred to as Maxwell-Wagner polarization.  
 263 This polarization mechanism is related to the discontinuity of displacement currents at  
 264 interfaces of porous composites. According to Revil (2013), Maxwell-Wagner polarization is  
 265 not negligible but not as important as often emphasized in the technical literature. We  
 266 acknowledge that this mechanism should be included in future studies.

267 In the next section, we discuss the properties of the tortuosity and formation factor  
 268 tensors and describe their definition for anisotropic porous material.

269

## 270 FORMATION FACTOR AND TORTUOSITY TENSORS

271 We first invoke the definition of two textural parameters,  $F$  and  $\Lambda$ , defined in a number  
 272 of previous studies (e.g., Johnson et al., 1986; Avellaneda and Torquato 1991; Pride, 1994).  
 273 The canonical boundary value problem for the normalized potential  $\Gamma$  of a cylindrical  
 274 representative elementary volume of porous material of length  $L$  can be written as

$$275 \quad \nabla^2 \Gamma = 0 \text{ in } V_p, \quad (30)$$

$$276 \quad \hat{\mathbf{n}}_s \cdot \nabla \Gamma = 0 \text{ on } S, \quad (31)$$

277 and

$$278 \quad \Gamma = \begin{cases} L & \text{at } z = L \\ 0 & \text{at } z = 0 \end{cases} \text{ on } S, \quad (32)$$

279 where  $z$  denotes the distance along the axis of the cylindrical core. In the above equations,  $\hat{\mathbf{n}}_s$   
 280 denotes the unit vector normal to the pore water/mineral interface,  $S$  (directed from the pore to  
 281 the solid phase, Figure 1), and  $V_p$  designates pore volume. Boundary conditions defining the  
 282 normalized potential  $\Gamma$  are representative for the injection of an electrical current into a rock

283 sample in the absence of surface conduction along the pore/water interface (see Johnson et al.,  
 284 1986, Avellaneda and Torquato, 1991). The formation factor  $F$  is defined as (Johnson et al.,  
 285 1986)

$$286 \quad \frac{1}{F} = \frac{1}{V} \int_{V_p} |\nabla\Gamma|^2 dV_p, \quad (33)$$

287 where  $V$  is the total volume of the considered representative elementary volume. Similarly,  
 288 the tortuosity of the pore space is defined by Pride (1994) as

$$289 \quad \frac{1}{\tau} = 1 + \frac{\hat{\mathbf{z}}}{V_p} \cdot \int_S \hat{\mathbf{n}}_s \Gamma dS, \quad (34)$$

290 where the integration is performed over the surface of the grain/pore water interface,  $S$ .  
 291 Similarly, surface tortuosity could be defined from the surface formation factor introduced by  
 292 Revil and Glover (1997). However, such surface tortuosity is required in our model for the  
 293 reasons explained above.

294 In what follows, we designate  $\mathbf{e} = -\nabla\Gamma$  the normalized electrical field (local electrical  
 295 field divided by the norm of the macroscopic imposed field). The previous set of definitions  
 296 can be readily generalized to the anisotropic case in the following manner:

$$297 \quad \mathbf{F} = \frac{1}{V} \int_{V_p} \mathbf{e} \otimes \mathbf{e} dV_p, \quad (35)$$

298 and

$$299 \quad \mathbf{T} = \frac{1}{V_p} \int_{V_p} \mathbf{e} \otimes \mathbf{e} dV_p, \quad (36)$$

300 Equations 35 and 36 show that  $\mathbf{F}$  and  $\mathbf{T}$  are symmetric.

301 Tortuosity and formation factor tensors can also be written in terms of three  
 302 eigenvalues  $T^i$  (positive and less than one) for  $\mathbf{T}$  and  $(1/F^i)$  ( $F_i$  positive and greater than one)  
 303 for  $\mathbf{F}$  and the eigenvectors  $\mathbf{t}^i$  as

$$304 \quad \mathbf{T} = \sum_{i=1}^3 T^i \mathbf{t}^i \otimes \mathbf{t}^i, \quad (37)$$

305 and

$$306 \quad \mathbf{F} = \sum_{i=1}^3 \left( \frac{1}{F^i} \right) \mathbf{t}^i \otimes \mathbf{t}^i. \quad (38)$$

307 For isotropic media, the above formulations simplify to the classical tortuosity and formation  
308 factor (see Bear, 1988 for a description of the connectivity tensor),

$$309 \quad T^1 = T^2 = T^3 = \frac{1}{\tau}, \quad (39)$$

310 and

$$311 \quad F^1 = F^2 = F^3 = \frac{\tau}{\phi}. \quad (40)$$

312 The inverses of connectivity and conductivity formation factor tensors are obtained through  
313 the expressions

$$314 \quad \mathbf{T}^{-1} = T_{ij}^{-1} \mathbf{e}_i \otimes \mathbf{e}_j = \sum_{i=1}^3 \frac{1}{T^i} \mathbf{t}^i \otimes \mathbf{t}^i, \quad (41)$$

315 and

$$316 \quad \mathbf{F}^{-1} = F_{ij}^{-1} \mathbf{e}_i \otimes \mathbf{e}_j = \sum_{i=1}^3 F^i \mathbf{t}^i \otimes \mathbf{t}^i, \quad (42)$$

317 respectively. Note that for TI media, with (1,2) being the symmetry plane, one has

$$318 \quad F^1 = F^2 \neq F^3 \quad \text{and} \quad T^1 = T^2 \neq T^3. \quad \text{The anisotropy ratio is defined as } \lambda = F^3 / F^1 = T^3 / T^1.$$

319 Mudrock formations are expected to have a petrofabric obeying this type of symmetry. In

320 such a case, our model predicts that the anisotropy ratio for in-phase conductivity should be

321 the same as that of quadrature conductivity. In addition, the anisotropy ratio for formation

322 factor should be the same for both surface and quadrature conductivities. We verify this

323 prediction in the last section of the paper.

324 **INFLUENCE OF ORGANIC MATTER AND KEROGEN CONTENT ON**  
 325 **COMPLEX CONDUCTIVITY**

326 As emphasized above, CEC plays a critical role in controlling not only the surface  
 327 conductivity of clayey materials (Waxman and Smits, 1968), but also their quadrature  
 328 conductivity (Vinegar and Waxman, 1984; Revil, 2012), or equivalently the low-frequency  
 329 dielectric constant (Josh et al., 2012; Revil, 2013). This behavior is illustrated in Figure 2 for  
 330 the quadrature conductivity of porous siliciclastic materials.

331 In our model, quadrature conductivity can be expressed as a function of CEC as

$$332 \quad \sigma'' = -\mathbf{b} \text{CEC}_M, \quad (43)$$

333 and

$$334 \quad \mathbf{b} = \beta_{(+)}^S f \rho_s \mathbf{T}. \quad (44)$$

335 For isotropic and kerogen-free materials, Figure 2 plots equation 43 with  $\mathbf{b} = b\mathbf{I}$  ( $\mathbf{I}$  denotes  
 336 the identity  $3 \times 3$  matrix) and  $b = 2.38 \times 10^{-7} \text{ S kg C}^{-1} \text{ m}^{-1}$  ( $F\phi$  has been replaced by a tortuosity  
 337 of  $3/2$ , roughly the tortuosity of a path around spherical grains) against measurements. For  
 338 fine-grained shales, tortuosity is expected to be much higher than 1.5. The last section of this  
 339 paper shows that the tortuosity of bulk pore space of a mudrock can exceed 100. In turn, this  
 340 behavior implies that for the same CEC, the quadrature conductivity of a mudrock is much  
 341 smaller than for the case of a porous shaly sand (typically 1.5 to 3, see Vinegar and Waxman,  
 342 1984). Such an observation will also be discussed in the last section of the paper.

343 In Figure 3, we also test the fact that, according to our model, the salinity dependence  
 344 of quadrature conductivity is governed by the salinity dependence of the partition coefficient,  
 345  $f$ . This salinity dependence is discussed in Appendix A. As  $f$  increases with salinity, we  
 346 expect the magnitude of the quadrature conductivity to increase with salinity in agreement

347 with what is shown in Figure 3 (see also Weller et al., 2011; Revil and Skold, 2012; Weller  
348 and Slater, 2012; and Revil et al., 2013).

349 In mudrocks (or in soils rich in organic matter), one may wonder about the role of  
350 kerogen or humic substances on complex conductivity. Kerogens are commonly present in  
351 high concentration in mudrocks, which clearly indicates they are potential source rocks for  
352 hydrocarbon deposits. However, this also indicates the solid phase comprises an additional  
353 component, which is characteristically distinct from the mineral rock matrix and should be  
354 accounted for in the analysis of complex conductivity.

355 To understand the CEC or specific surface area (SSA or  $S_{sp}$ ) of kerogen-rich rocks, it  
356 is important to emphasize the CEC or specific surface area of the kerogen itself. Few  
357 published works have considered the CEC / specific surface area measurements in oil or gas  
358 mudrocks. In that context, Derkowski and Bristow (2012) addressed the important question  
359 of whether sedimentary organic matter (mostly kerogen) in oil and gas mudrocks exhibits  
360 similar properties to those of organic matter found in soils. Indeed, during burial, organic  
361 matter has been subjected to pressure and temperature changes and these changes can alter the  
362 original properties.

363 Helling et al. (1964) reported a CEC for organic matter in soils, for pH between 6 to 8,  
364 in the range 1.6 to 2.1 meq g<sup>-1</sup> [1 meq g<sup>-1</sup> = 96,320 C kg<sup>-1</sup>, equating to (1.5-2.0)×10<sup>5</sup> C kg<sup>-1</sup> in  
365 SI units]. Kaiser et al. (2007) reported CEC values for organic matter of soils in the order of  
366 (0.3-3.5)×10<sup>5</sup> C kg<sup>-3</sup> at pH 7. These values are extremely high and similar to the cation  
367 exchange capacity of smectite (about 1 meq g<sup>-1</sup>, 10<sup>5</sup> C kg<sup>-3</sup>, e.g., Revil, 2012), the clay  
368 mineral with the highest cation exchange capacity. Humus is known to have a CEC greater  
369 than smectite. This cation exchange capacity is explained by the high reactivity of the surface  
370 of organic matter as well as by the existence of isomorphic substitution in the organic  
371 macromolecules themselves (such as with smectite). Figure 4 shows different reactive sites



372 on the surface of organic matter that are responsible for their high CEC. At near neutral pH  
 373 values, the number of electrical charges per unit surface area can be determined as the ratio of  
 374 total charge per unit mass CEC to total surface area per unit mass SSA; for humus: 559 cMol  
 375 kg<sup>-1</sup> (5.6×10<sup>5</sup> C kg<sup>-3</sup>) by 7.2 x 10<sup>5</sup> m<sup>2</sup> kg<sup>-1</sup>; this yields a surface charge of 0.78 C m<sup>-2</sup> (about 5  
 376 elementary charge per nm<sup>2</sup>), a value that is approximately twice that of clays (e.g., Woodruff  
 377 and Revil, 2011).

378 The CEC and specific surface area of soil or oil mudrocks can therefore be written as

$$379 \quad \text{CEC} = \sum_{i=1}^N \chi_i \text{CEC}_i, \quad (46)$$

380 and

$$381 \quad S_{sp} = \sum_{i=1}^N \chi_i S_{sp,i}, \quad (47)$$

382 where  $N$  is the number of the mineral phases (including kerogen in oil mudrocks or organic  
 383 matter in soils) and  $\chi_i$  denotes the mass fraction of the  $i$ -th mineral with respect to the total  
 384 mass of dry solid. In oil mudrocks, CEC can be expected to be dominated by clay minerals  
 385 and kerogen, whereby

$$386 \quad \text{CEC} = \chi_K \text{CEC}_K + \chi_I \text{CEC}_I + \chi_S \text{CEC}_S + \chi_{Ke} \text{CEC}_{Ke}, \quad (48)$$

387 and

$$388 \quad S_{sp} = \chi_K S_{sp,K} + \chi_I S_{sp,I} + \chi_S S_{sp,S} + \chi_{Ke} S_{sp,Ke}, \quad (49)$$

389 where the subscripts K, I, and S refer to kaolinite, illite, and smectite, respectively, while Ke  
 390 refers to kerogen. There are five types of kerogen defined in the literature: Type I (sapropelic,  
 391 formed from protein and lipids of mostly algae), Type II (Planktonic, formed from lipids of  
 392 plankton deposited under reducing conditions), Type II-S (similar to type II with a high sulfur  
 393 content), Type III (humic, from terrestrial plants), and Type IV (contains mostly decomposed

394 organic matter). It is possible that the CEC and SSA of kerogen may depend on the type and  
395 maturity of kerogen as well.

396         The CEC of humic matter and kerogen can be related to the quantity of carbon in oil  
397 mudrocks. For soils that are rich in organic matter, it is known that cation exchange capacity  
398 is highly correlated with carbon content (Figure 5). Therefore, one could expect a correlation  
399 between TOC (total amount of organic carbon content in weight %) of kerogen and cation  
400 exchange capacity of the material. That said, experimental results available in the literature  
401 are conflicting (see the discussion in Derkowski and Bristow, 2012). The CEC of kerogen is  
402 believed to be very small compared to the CEC of organic matter in soils because all the  
403 available exchangeable sites in functional groups shown in Figure 4 may have been  
404 polymerized during burial (see Vandembroucke and Largeau, 2007). Derkowski and Bristow  
405 (2012) indicate that the thermal treatment used prior to CEC measurements can reactivate  
406 some of these functional sites (possibly through the deprotonation of carboxylic acids) and  
407 lead to a CEC associated with kerogen which may explain conflicting results found in the  
408 literature. Derkowski and Bristow (2012) observed an inverse relationship between kerogen  
409 maturity and the amount of carboxylic groups. It then follows that immature kerogen has  
410 greater susceptibility to thermal activation. Therefore, the thermal treatment applied to less  
411 mature kerogen may substantially increase the CEC of the material, as well as surface  
412 conduction and quadrature conductivity (polarization).

413         In summary, we believe that the CEC of kerogen can be neglected in the evaluation of  
414 the quadrature conductivity of hydrocarbon-bearing tight mudrocks (Derkowski and Bristow,  
415 2012) but not the specific surface area, which can be very high. Derkowski and Bristow  
416 (2012) reported a specific surface area in the range from 700 to 920 m<sup>2</sup> g<sup>-1</sup> for kerogen  
417 extracted from the mature Red Bird and Monterey formations. This represents a range of  
418 values very similar to that measured for smectite (e.g., Woodruff and Revil, 2011). For the

419 Woodford formation, Derkowski and Bristow (2012) measured the excess specific surface  
 420 area not accounted for by clay minerals. As shown in Figure 6, such an excess surface area is  
 421 correlated with total amount of organic carbon content (in weight %). The relationship can be  
 422 written as

$$423 \quad S_{sp}(\text{Kerogen}) = a \text{TOC}(\%), \quad (50)$$

424 where  $a \approx 10$ . For pure kerogen, the above expression yields [ $\text{TOC}(\%) = 100$ ] a specific  
 425 surface area of  $1000 \text{ m}^2 \text{ g}^{-1}$ , which is only slightly higher than values given above. Therefore,  
 426 specific surface area is given by

$$427 \quad S_{sp} = \chi_{\text{Clay}} S_{sp,\text{clay}} + S_{sp,\text{Ke}} \text{TOC}, \quad (51)$$

428 where TOC is expressed in mass fraction (in %). However, it is unclear at this point whether  
 429 kerogen would impact the quadrature conductivity through its surface area. In principle, if  
 430 there is no Stern layer associated with kerogen (no reactive sites), presence of kerogen in oil  
 431 and gas mudrocks should have no impact on quadrature conductivity. Therefore if the  
 432 specific surface area is used to assess the quadrature conductivity, the former should be  
 433 corrected for the contribution of kerogen. The TOC content might also change the tortuosity  
 434 of the porous body and indirectly affect the bulk conductivity. Furthermore, if bitumen is  
 435 present, the polar components might contribute to the surface conductivity. However, these  
 436 effects need to be verified by experimental evidence.

437

## 438 **COMPARISON TO EXPERIMENTAL DATA**

439

### 440 **Material and methods**

441 This section analyzes the complex conductivity of two Bakken core samples. The  
 442 Bakken formation is a Late Devonian Early Mississippian shale (deposited approximately 360  
 443 millions of years ago) located in the Williston Basin, underlying parts of Montana, North

444 Dakota, and Saskatchewan. Sample A was acquired at a depth of 2630 m while Sample B was  
445 acquired at 3098 m. The deeper sample, Sample B, is from the higher-temperature, central  
446 portion of the Williston Basin, whereas the second core sample is from the basin's margin.  
447 Table 1 summarizes the properties of the two core samples. Porosity was measured by  
448 hydrogen adsorption, which does not account for the percentage weight (wt%) of kerogen;  
449 20wt% kerogen results in 40-70 vol% kerogen, depending on the density of kerogen (Prasad  
450 et al., 2011). Average non-kerogen porosity in Bakken shale samples is approximately 3%.

451 Spectral induced polarization measurements were performed using an apparatus  
452 developed at the Central Laboratory for Electronics, ZEL, at the Forschungszentrum Jülich, in  
453 Germany by Zimmermann et al. (2008). Various tests of this impedance meter have been  
454 documented by Revil and Skold (2011) and will not be repeated here. Electrodes used were  
455 sintered Ag/AgCl<sub>2</sub> 2 mm pellet electrodes for voltage measurements ([http://www.science-](http://www.science-products.com/Products/CatalogG/IVM-AgAgCl2-Pellets/ivm.html)  
456 [products.com/Products/CatalogG/IVM-AgAgCl<sub>2</sub>-Pellets/ivm.html](http://www.science-products.com/Products/CatalogG/IVM-AgAgCl2-Pellets/ivm.html)), and transcutaneous  
457 electrical nerve stimulation (TENS) adhesive electrodes  
458 (<https://www.djoglobal.com/products/chattanooga/dura-stick-ii-self-adhesive-electrodes>) for  
459 current injection (see Figure 7 for a description of the position of the electrodes).

460 The Bakken samples were saturated with three pore-water solutions of varied salinity  
461 derived from an equilibrium solution obtained by saturating (distilled) DI water with a soluble  
462 mineral fraction of pulverized core fragments. A low-salinity limit of 0.5 mM was estimated  
463 as the equilibrium concentration of NaCl. Solutions were also prepared for 0.05 M and 0.5 M.  
464 The samples were initially saturated with equilibrium water under sequential pressurizations  
465 up to 10.3 MPa (1500 psi), and re-saturated with the remaining solutions in two stages.  
466 Spectral induced polarization acquisitions were made at each of the three stages. Due to the  
467 low diffusion coefficient for the NaCl solution in the samples, approximately  $10^{-11} \text{ m}^2\text{s}^{-1}$   
468 (Revil et al., 2005), the equilibration time at each stage is in the order of several weeks (the

469 average radius of the cylindrical samples is 0.010 m, yielding  $1 \times 10^{-4} / 2.5 \times 10^{-11} = 4 \times 10^6 \text{ s} \approx$   
470 46 days). The brine is degassed prior to the saturation. The saturated samples are immersed  
471 in the respective equilibrium solution and stored at low pressure close to vacuum conditions.

472         Complex spectra of the eigenvalues of the electrical impedance tensor were obtained  
473 directly by following the single-component polarization protocol with the 4 electrode  
474 impedance spectroscopy method developed by Zimmermann et al. (2008). The Bakken B  
475 specimens are cylindrical cores with a radius of 12.6 mm and heights 38.3 mm and 30.8 mm  
476 for the in-plane and transverse directions, respectively; geometric factors were obtained  
477 numerically using a Comsol Multiphysics simulator. We perform the measurements at  
478 laboratory temperature and pressure; we coated the samples in quick dry nail polish to prevent  
479 both evaporation at the core surface, as well as impose an insulating boundary, constituting a  
480 closed electrical system for the measurements. With this approach, no sample holder is  
481 required. The coating is easily removed with acetone to maximize surface exposure for  
482 subsequent pressurizations. Spectral complex conductivity tensors were determined from the  
483 measured directional impedances of the samples. Table 2 summarizes the in-phase and  
484 quadrature conductivity of the two core samples at 1 Hz.

485         We also performed spectral induced polarization at five different stages, referred to  
486 below as stages I through V, during the pressurized saturation sequence, capturing unsaturated  
487 measurements at different water contents for Sample B. The samples were pressurized at  
488 increasing sequential maximum confining (hydrostatic) pressures of 0.69 MPa, 3.45 MPa,  
489 6.89 MPa, and 10.34 MPa. Stages I and II were completed in two successive 24 hour periods,  
490 and stages III and IV in successive 48 hour periods. An additional measurement was made  
491 after 30 days to represent the final saturation state, stage V (the datasets of stages IV and V  
492 are equivalent, evidencing full saturation of the sample; the stage V measurements are used in

493 our analysis). The water content is determined through gravimetric monitoring at each  
494 saturation stage.

495

#### 496 **Results under saturated conditions**

497 Figure 8 shows the raw data for the phase. The tangent of the phase angle is defined  
498 as the ratio of quadrature conductivity to in-phase conductivity. Figure 8 reveals only a fair  
499 agreement between the phases measured in the in-plane and transverse directions of the core  
500 samples at low frequencies. The magnitude of the phase increases slightly with frequency  
501 below 100 Hz and faster above 100 Hz. The polarization of the electrical double layer is  
502 expected to dominate the response of the quadrature conductivity below 100 Hz, while above  
503 100 Hz, the response is partly controlled by the true dielectric polarization of the material  
504 with some influence from the Maxwell-Wagner polarization (see Revil, 2013) and possibly  
505 some electromagnetic coupling effects.

506 The complex conductivity spectra are plotted as a function of frequency for the three  
507 salinities in Figure 9 for Sample A, and in Figure 10 for Sample B. In-phase conductivity  
508 data display only weak dependence with respect to frequency as already observed for other  
509 clay-rich materials (see Vinegar and Waxman, 1984; Slater and Lesmes, 2002; Revil, 2012).  
510 Quadrature conductivity spectra exhibit a plateau at low frequencies and an increase in  
511 magnitude at high frequencies due to Maxwell-Wagner polarization and true dielectric  
512 polarization (Revil, 2013).

513 We first test our prediction regarding anisotropy ratio for in-phase and quadrature  
514 conductivities (see Figure 11). The mean anisotropy ratio is  $8.1 \pm 3.1$  ( $N = 12$ ,  $N$ : number of  
515 measurements) for in-phase and quadrature conductivity data acquired together for the two  
516 core samples ( $7.6 \pm 2.3$ ,  $N = 6$ , for the in-phase conductivity and  $8.5 \pm 3.8$ ,  $N = 4$ , for the  
517 quadrature conductivity). The anisotropy ratio is approximately the same for both in-phase  
518 and quadrature conductivities. This behavior is consistent with the predictions of our model.

519 We now focus on the relationship between in-phase conductivity and pore water  
 520 conductivity of NaCl solutions. Electrical conductivity of water can be described using the  
 521 semi-empirical relation derived by Sen and Goode (1992), i.e.

$$522 \quad \sigma_f(C_f; T) = (d_1 + d_2 T + d_3 T^2) C_f - \frac{d_4 + d_5 T}{1 + d_6 C_f} (C_f)^{3/2}, \quad (52)$$

523 where  $d_1 = 5.6$ ,  $d_2 = 0.27$ ,  $d_3 = -1.51 \times 10^{-4}$ ,  $d_4 = 2.36$ ,  $d_5 = 0.099$ ,  $d_6 = 0.214$ ,  $\sigma_f$  is electrical  
 524 conductivity of water (in  $\text{S m}^{-1}$ ),  $T$  is temperature (in  $^\circ\text{C}$ ) and  $C_f$  is salinity (in  $\text{M}$ ,  $\text{mol L}^{-1}$ ).  
 525 This relation yields pore water conductivities of  $3.82 \text{ S m}^{-1}$ ,  $0.49 \text{ S m}^{-1}$ , and  $0.0054 \text{ S m}^{-1}$ .  
 526 Figure 11 shows the corresponding in-phase and quadrature conductivities as a function of  
 527 conductivity of pore water solution. The relationship between in-phase conductivity and pore  
 528 water conductivity is used to determine formation factor and surface conductivity in the in-  
 529 plane and transverse directions with respect to bedding plane. Table 3 reports the formation  
 530 factors and surface conductivities, together with the determination of Archie's porosity  
 531 exponent ( $m = -\ln F / \ln \phi$  in the two directions) and tortuosity ( $\tau = F\phi$ ). For Samples A and  
 532 B, the surface conductivity anisotropy ratios are  $8.8 \pm 0.9$  and  $7.4 \pm 0.8$ , respectively. These  
 533 values are comparable to the anisotropy ratios for the quadrature conductivity,  $6.3 \pm 0.7$  and  
 534  $6.8 \pm 0.8$ , respectively for Samples A and B.

535 The immature sample A may have higher clay content, which could explain the higher  
 536 surface conductivity than observed for sample B. Regarding quadrature conductivity, the in-  
 537 plane (I) and transverse (T) quadrature conductivities are given by

$$538 \quad \sigma''(I) = -\frac{\beta_{(+)}^S f \rho_s}{\tau_I} \text{CEC}_M, \quad (53)$$

539 and

$$540 \quad \sigma''(T) = -\frac{\beta_{(+)}^S f \rho_s}{\tau_T} \text{CEC}_M, \quad (54)$$

541 while surface conductivities in the in-plane and transverse directions are given by

542 
$$\sigma_s(I) = \frac{\rho_s \beta_{(+)}(1-f)}{\tau_I} \text{CEC}_M, \quad (55)$$

543 and

544 
$$\sigma_s(T) = \frac{\rho_s \beta_{(+)}(1-f)}{\tau_T} \text{CEC}_M, \quad (56)$$

545 respectively, where  $\beta_{(+)}(\text{Na}^+, 25^\circ\text{C}) = 5.2 \times 10^{-8} \text{ m}^2\text{s}^{-1}\text{V}^{-1}$ ) and  $\beta_{(+)}^s(25^\circ\text{C}, \text{Na}^+) = 1.5 \times 10^{-10}$   
 546  $\text{m}^2\text{s}^{-1}\text{V}^{-1}$  for clay minerals (Revil, 2012, 2013). We first determine the CEC using equations  
 547 53 and 54, and  $f$  close to 1. Very consistent values are obtained at high salinities with  $\text{CEC} =$   
 548  $2500 \pm 300 \text{ C kg}^{-1}$  for sample A and  $\text{CEC} = 1200 \pm 300 \text{ C kg}^{-1}$  for sample B. This behavior  
 549 agrees with the known CEC of the Bakken shale, which is in the order of  $10^{-2}$  to  $10^{-1} \text{ meq g}^{-1}$   
 550 (about 1000 to 10,000  $\text{C kg}^{-1}$ ; data obtained from the North Dakota Industrial Commission,  
 551 Department of Mineral Resources, Oil and Gas Division online subscription database,  
 552 <https://www.dmr.nd.gov/oilgas/subscriptionservice.asp>). Using equations 55 and 56, we  
 553 obtain  $f = 0.78 \pm 0.03$  for Sample A and  $f = 0.99$  for Sample B. The values of CEC and  $f$   
 554 obtained by our model are consistent with the expected their respective relationship to clay  
 555 type, and may imply that sample A is richer in smectite and that Sample B is rich in kaolinite.

556 Figure 12 describes the impact of anisotropy and increase of tortuosity for the Bakken  
 557 shale by comparison to shaly sands investigated by Vinegar and Waxman (1984) and the  
 558 saprolites investigated by Revil et al. (2013). As predicted by our model, at given values of  
 559 CEC and salinity, the magnitude of quadrature conductivity is expected to decrease with the  
 560 increase of tortuosity and differ in the in-plane and transverse directions (relative to  
 561 bedding. Tortuosity in the in-plane direction is also found to be much smaller than in the  
 562 transverse direction. As shown in Figure 13a, differential compaction during burial is  
 563 responsible for the formation of a bedding plane with the shale, thereby becoming a TI  
 564 medium. In this case, we expect the tortuosity in the in-plane direction to be substantially



565 smaller than in the transverse direction (Figure 13b). Tortuosity in this case can also be  
566 related to the aspect ratio of grains, as discussed in Mandelson and Cohen (1982). Other  
567 published experimental works have reported very high tortuosities; for instance Revil et al.  
568 (1996) reported tortuosities in the range of 2 to 46 for doleritic core samples. Zhang and  
569 Scherer (2012, their Table 6) have reported electrical tortuosities in the range 2 to 118 for  
570 tight shales. Values higher than 100 were obtained for very tight specimens with porosities  
571 below 3%.

572

### 573 **Results Under Unsaturated Conditions**

574 Figure 14 shows the in-phase and quadrature conductivities of Sample B at different  
575 saturations. It is clear from this figure that saturation does not change the anisotropy ratio of  
576 the material. In-phase and quadrature conductivity data are plotted as a function of saturation  
577 in Figure 15. Measurements are fitted with a power-law relationship to determine the  
578 saturation  $n$ -exponent and the  $p$ -exponent describing the saturation dependence of quadrature  
579 conductivity. The first observation is that the  $n$  and  $p$  exponents do not exhibit significant  
580 anisotropy ( $n = 2.7 \pm 0.4$  in the in-plane direction and  $n = 2.4 \pm 0.3$  in the transverse direction  
581 and  $p = 1.8 \pm 0.1$  in the in-plane direction and  $p = 1.4 \pm 0.2$  in the transverse direction). Figure  
582 16 reports the values of the two exponents together with the  $n$  and  $p$  exponents of isotropic  
583 sedimentary materials (see Revil, 2013). All the data conform fairly well to the general trend  
584  $p = n - 1$ .

585

586

## CONCLUSIONS

587 We introduced a new petrophysical model to describe the complex electrical  
588 conductivity tensor of oil mudrocks. The model accounts for anisotropy, saturation, porosity,  
589 and cation exchange capacity/specific surface area of rocks. Verification experiments were

590 performed on two core samples from the Bakken formation. The following conclusions stem  
591 from the work presented in this paper:

592 (1) In-phase electrical conductivity is controlled by a formation factor tensor while  
593 quadrature conductivity is controlled by a tortuosity tensor of the bulk pore space. Both  
594 tensors are interrelated through the connected porosity.

595 (2) The CEC of kerogen is believed to be very small in comparison to the CEC of  
596 organic matter in soils. Indeed, because of diagenesis, all the exchangeable sites in the  
597 functional groups of organic matter may have been polymerized; therefore, the surface of  
598 kerogen may not impact both surface and quadrature conductivity of oil and gas mudrocks.

599 (3) Experimental data confirmed our model prediction that the anisotropy ratio is the  
600 same for in-phase and quadrature conductivities. It was also confirmed that the anisotropy  
601 ratio is the same for formation factor and surface conductivity. The anisotropy ratio for the  
602 complex conductivity tensor is  $8.1 \pm 3.1$  for the two Bakken core samples. Our model predicts  
603 an invariant phase angle for both in-plane (I) and transverse (T) measurements for all  
604 frequencies. This behavior is only approximately shown by experimental data acquired at  
605 low frequencies; additional data will be needed for verification.

606 (4) Measurements performed on two rock samples from the Bakken formation indicate  
607 that our model provides a simple explanation for (a) the dependence of quadrature  
608 conductivity on salinity and (b) the effect of increase of tortuosity on the decrease of the  
609 magnitude of quadrature conductivity. The bulk tortuosity in the direction transverse to  
610 bedding plane is found to be higher than 100. This very high value of tortuosity is likely  
611 associated with the aspect ratio of grains.

612 (5) The decrease of saturation does not significantly change the degree of anisotropy  
613 observed for the quadrature and in-phase conductivities under saturated conditions. It follows

614 that the  $p$ -exponent characterizing the saturation dependence of quadrature conductivity can  
615 be related to the saturation exponent  $n$  by  $p = n-1$ .

616

617 **Acknowledgments.** This work was funded by The University of Texas at Austin's Research  
618 Consortium on Formation Evaluation, jointly sponsored by Anadarko, Apache, Aramco,  
619 Baker-Hughes, BG, BHP Billiton, BP, Chevron, China Oilfield Services, LTD.,  
620 ConocoPhillips, ENI, ExxonMobil, Halliburton, Hess, Maersk, Marathon Oil Corporation,  
621 Mexican Institute for Petroleum, Nexen, ONGC, Petrobras, Repsol, RWE, Schlumberger,  
622 Shell, Statoil, Total, and Weatherford. We also thank the Oclassh research project and its  
623 sponsor (Chevron, Repsol, Whiting, Venoco, Shell, Aramco, Magrtek, and Hess). We thank  
624 Egon Zimmermann for the construction of the impedance meter, Andreas Weller and an  
625 anonymous referee for their constructive reviews of our manuscript, and the Associate Editor  
626 for the speed of the review process.

627

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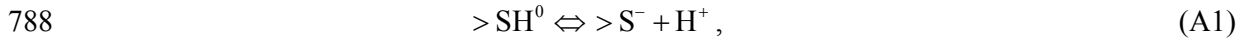


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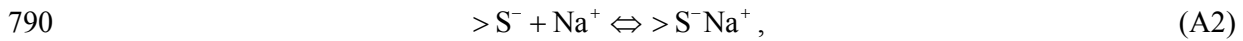
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783

784 **Appendix A**

785 We introduce a simple model to describe the dependence of salinity on the partition  
786 coefficient,  $f$ . Consider first the sorption of sodium in the Stern layer of clays and the  
787 dissociation of protons according to the following, simplified speciation model:



789 and



791

792 where  $>S$  designates the surface (amphoteric) sites attached to the crystalline framework,  $H^0$   
793 are protons (which are assumed to be immobile), while weakly sorbed  $Na^+$  (which are known  
794 to keep their hydration layer) are assumed mobile in the Stern layer. Equilibrium constants  
795 for the reactions A1 and A2 are given by,

796 
$$K_{Na} = \frac{\Gamma_{SNa}^0}{\Gamma_{S^-}^0 [Na^+]^0}, \quad (A3)$$

797 and

798 
$$K_H = \frac{\Gamma_{S^-}^0 [H^+]^0}{\Gamma_{SH}^0}. \quad (A4)$$

799 The conservation equation for the surface species is given by,

800 
$$\Gamma_S^0 = \Gamma_{SNa}^0 + \Gamma_{SH}^0 + \Gamma_{S^-}^0 + \Gamma_X^0, \quad (A5)$$

801 where  $\Gamma_S^0$  denotes the total surface site density (including charge associated with isomorphic  
802 substitutions in the crystalline framework),  $\Gamma_{SNa}^0$ ,  $\Gamma_{S^-}^0$ , and  $\Gamma_{SH}^0$  designate the surface charge  
803 density of the sites  $>S^-Na^+$ ,  $>S^-$ , and  $>SH^0$ , respectively, and  $\Gamma_X^0$  represents the number  
804 of equivalent sites corresponding to isomorphic substitutions (all expressed in sites  $m^{-2}$ ). To  
805 simplify notation, we write  $pH = -\log_{10} [H^+]$ , while  $[Na^+] = C_f$  denotes the salinity of the pore  
806 water solution. The resolution of equations equations A3 to A5 yields

807 
$$\Gamma_{SH}^0 = \frac{\Gamma_S^0 - \Gamma_X^0}{1 + \frac{K_H}{10^{-pH}} (1 + C_f K_{Na})}, \quad (A6)$$

808 
$$\Gamma_{S^-}^0 = \frac{(\Gamma_S^0 - \Gamma_X^0) K_H / 10^{-pH}}{1 + \frac{K_H}{10^{-pH}} (1 + C_f K_{Na})}, \quad (A7)$$

809 and

810 
$$\Gamma_{SNa}^0 = \frac{(\Gamma_S^0 - \Gamma_X^0) C_f K_{Na} K_H / 10^{-pH}}{1 + \frac{K_H}{10^{-pH}} (1 + C_f K_{Na})}. \quad (A8)$$

811 All the charged sites that are not compensated in the Stern layer need to be compensated in  
812 the diffuse layer. Therefore, the fraction of counterions in the Stern layer is defined by the  
813 equations

814 
$$f = \frac{\Gamma_{SNa}^0}{\Gamma_{SNa}^0 + \Gamma_{S^-}^0 + \Gamma_X^0}, \quad (A9)$$

815 and

816 
$$f = f_M \left\{ \frac{C_f K_{Na}}{f_M (1 + C_f K_{Na}) + (1 - f_M) \left[ 1 + C_f K_{Na} + \frac{10^{-pH}}{K_H} \right]} \right\}, \quad (A10)$$

817 where  $f_M$  designates the highest value of  $f$  reached at high salinities, i.e.

818 
$$f_M = \lim_{C_f \gg 1/K_{Na}} f = 1 - \frac{\Gamma_X^0}{\Gamma_S^0}. \quad (A11)$$

819 The value of  $f_M$  is approximately 0.99 for kaolinite, 0.90 for illite, and 0.85 for smectite. At  
820 high pH values one has

821 
$$f \approx f_M \left( \frac{C_f K_{Na}}{1 + C_f K_{Na}} \right). \quad (A12)$$

822 Therefore, an increase of salinity is responsible for an increase of the partition coefficient,  $f$ ,  
823 which in turn is responsible for an increase of the magnitude of the quadrature conductivity  
824 (see Revil, 2012).

825

826 **Tables**

827

828 **Table 1.** Properties of the two core samples. Porosity is non-kerogen matrix porosity. The  
 829 reported density is bulk density (grain density is estimated at 2650 kg m<sup>-3</sup>). Reference depth:  
 830 Kelly bushing.

Sample	Depth (m)	$\phi$	Density (kg m <sup>-3</sup> )	TOC (wt%)	Hydrogen Index	Maturation
<b>Bakken A</b>	2630	0.028	1,990	20.1	584	II
<b>Bakken B</b>	3098	0.032	2,220	12.1	436	III

831

832 **Table 2.** In phase  $\sigma'$  and quadrature conductivity  $\sigma''$  at different salinities ("I" stands for in-  
 833 plane measurements while "T" stands for transverse measurements with respect to bedding  
 834 plane).

	0.5 mM		0.05 M		0.5 M	
	in-phase	quadrature	in-phase	quadrature	in-phase	quadrature
<b>Bakken A-I</b>	7.82E-03	2.91E-05	1.01E-02	3.46E-05	1.54E-02	6.59E-05
<b>Bakken A T</b>	8.87E-04	4.65E-06	1.17E-03	5.52E-06	1.96E-03	4.03E-06
<b>Bakken B-I</b>	3.33E-04	6.29E-06	1.53E-03	2.06E-05	3.15E-03	3.21E-05
<b>Bakken A-T</b>	4.73E-05	9.23E-07	1.53E-04	2.72E-06	9.22E-04	4.05E-06

835

836 **Table 3.** Formation factor,  $F$ , surface conductivity,  $\sigma_s$ , porosity exponent,  $m$ , and tortuosity,  $\tau$   
 837 ("I" stands for in-plane measurements while "T" stands for transverse measurements with  
 838 respect to bedding plane). The tortuosity in a given direction is determined by the product of  
 839 the formation factor times porosity.

Sample	$F(I)$	$F(T)$	$\sigma_s$ (I, $\times 10^{-4}$ S/m)	$\sigma_s$ (T, $\times 10^{-4}$ S/m)	$m(I)$	$m(T)$	$\tau(I)$	$\tau(T)$
<b>Bakken A</b>	543±100	3770±530	84±7	9.6±0.8	1.76	2.30	15.2	106
<b>Bakken B</b>	406±130	4350±30	3.2±0.8	0.43±0.03	1.75	2.43	13.0	139

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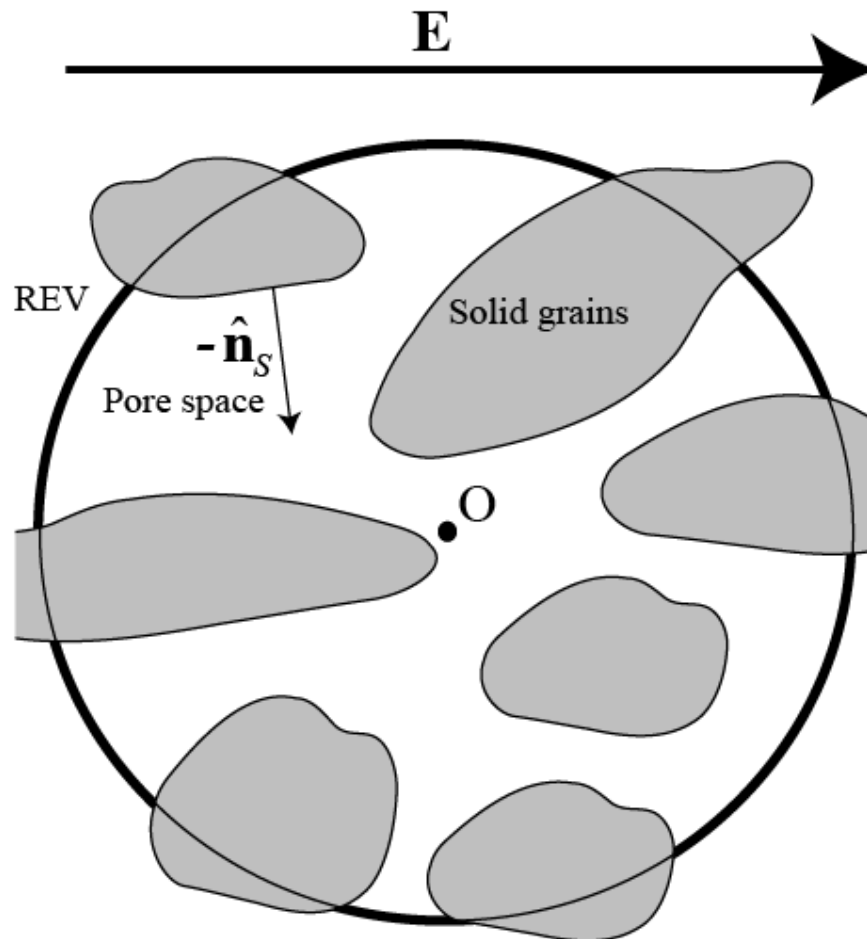
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## Figures

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846 **Figure 1.** Description of the Representative Elementary Volume (REV) centered at point O.

847 Vector  $\hat{n}_s$  denotes the unit vector locally normal to the grains,  $E$  denotes the macroscopic

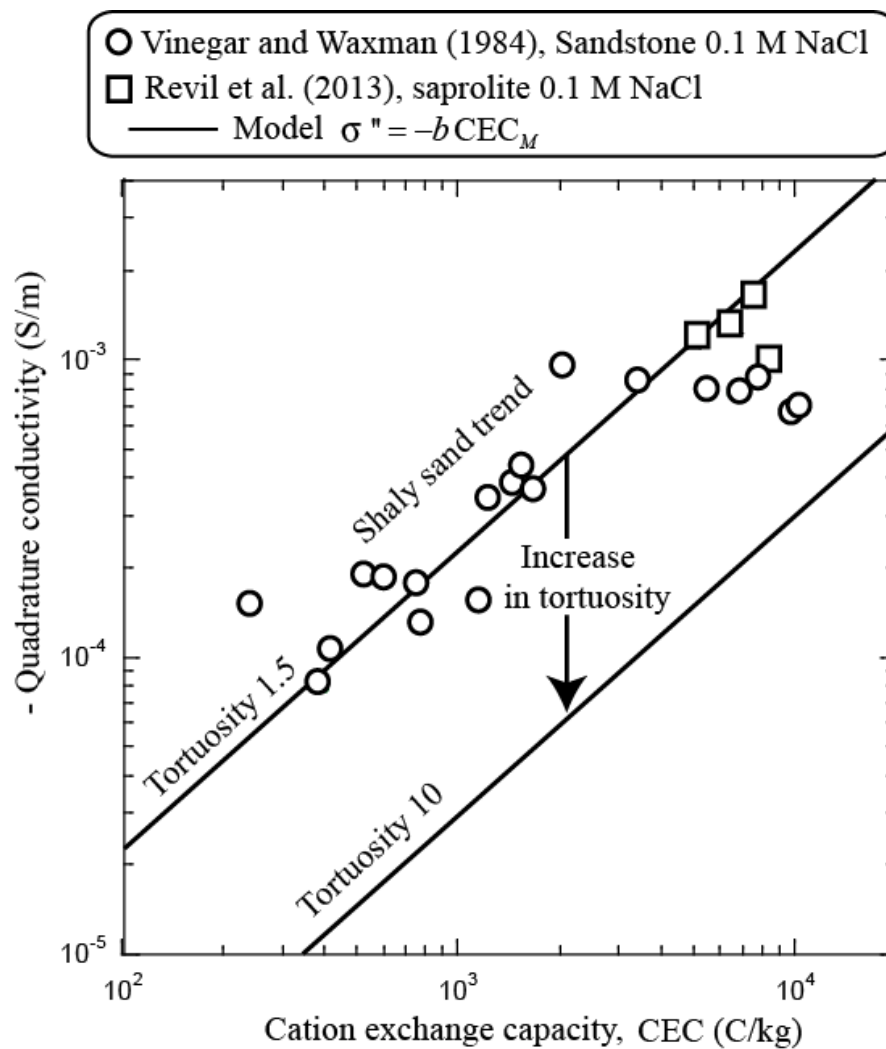
848 electrical field applied to the REV. The local electric field is written as  $e$  in the main text and,

849 in absence of electrical double layer, it is locally tangential to grain surfaces.

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855 **Figure 2.** Linear relationship between quadrature conductivity and cation exchange capacity  
 856 of clayey materials assuming fully saturated conditions (NaCl solution), equal salinity (0.1  
 857 M), same temperature, same frequency (approximately 10 Hz), and same pH range (5-7). The  
 858 solid line was calculated for a tortuosity of 1.5. Higher tortuosities would generate lines  
 859 parallel to the one shown but would predict smaller quadrature conductivity amplitudes for  
 860 the same values of CEC and salinity.

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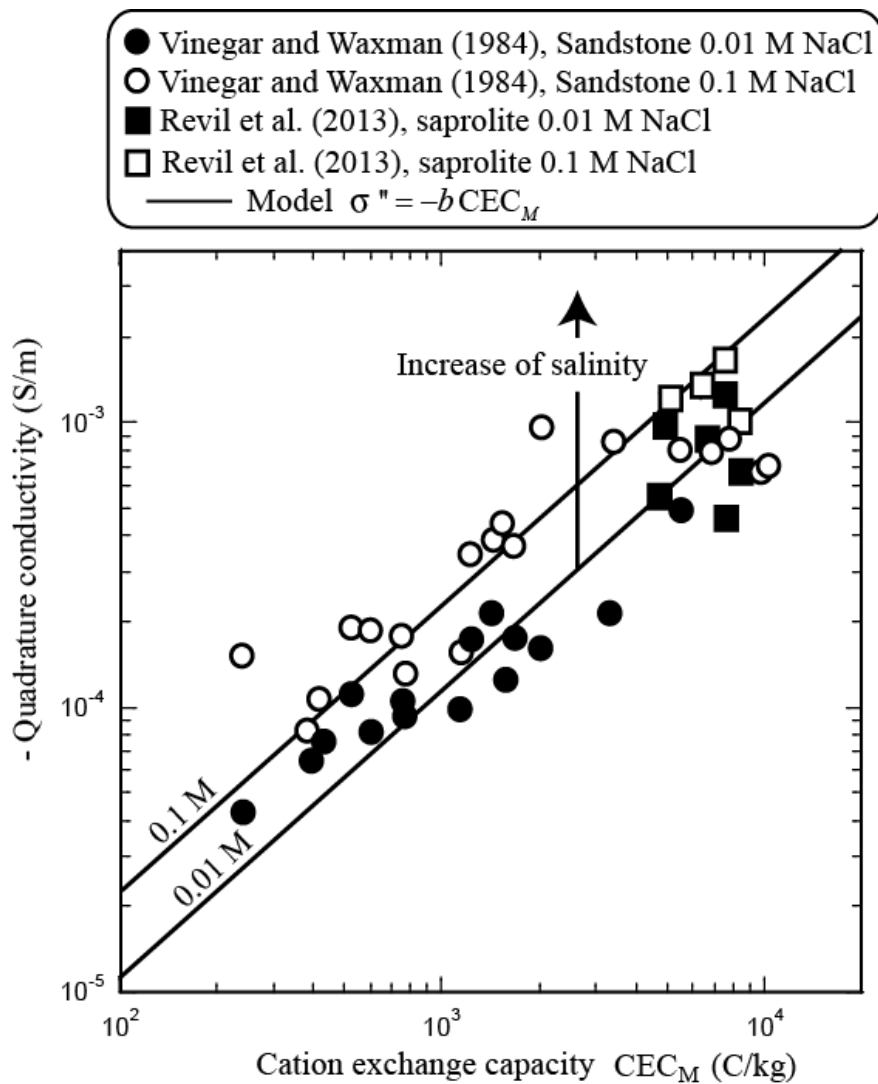
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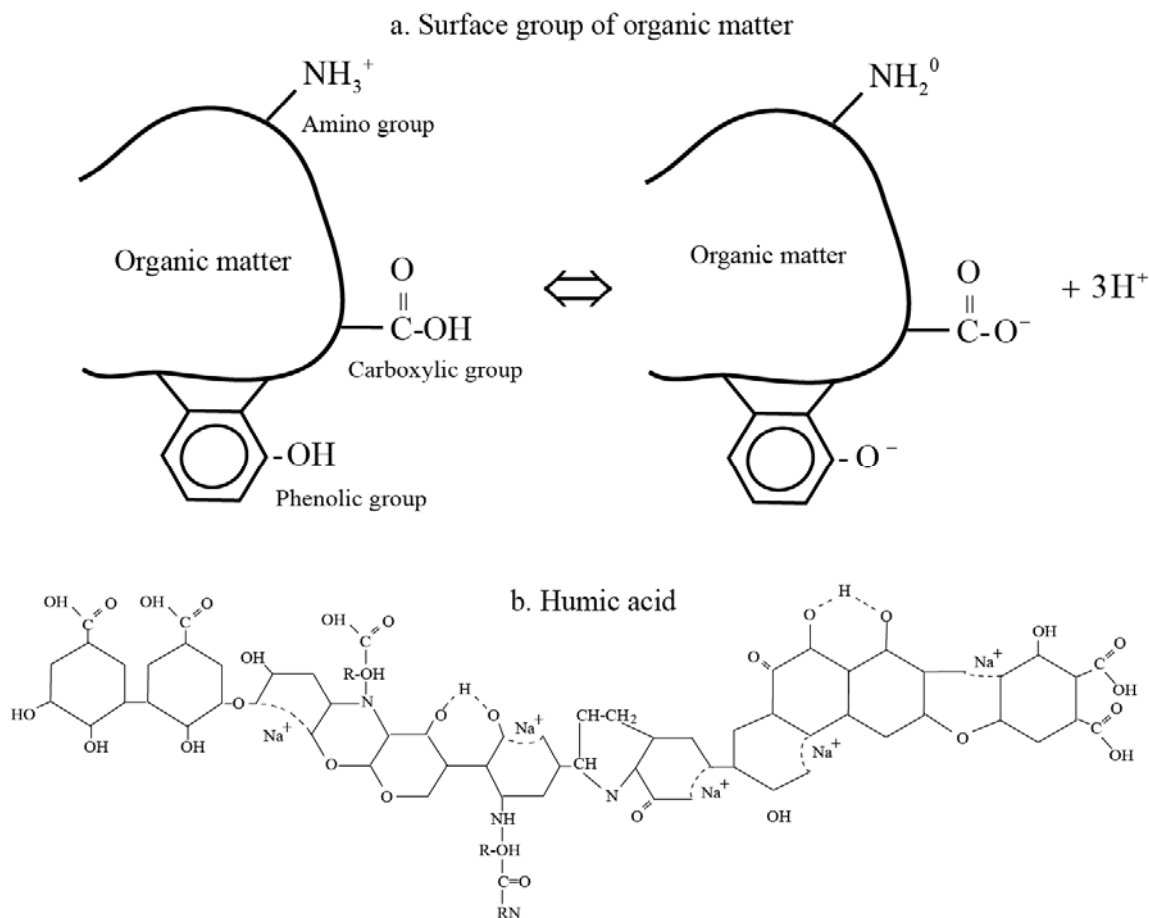


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868 **Figure 3.** Influence of the salinity on the magnitude of quadrature conductivity. The increase  
 869 of salinity is responsible for an increase of the magnitude of quadrature conductivity. In our  
 870 model, this effect is related to the effect of salinity on the partition coefficient,  $f$ , of  
 871 counterions in the Stern layer.

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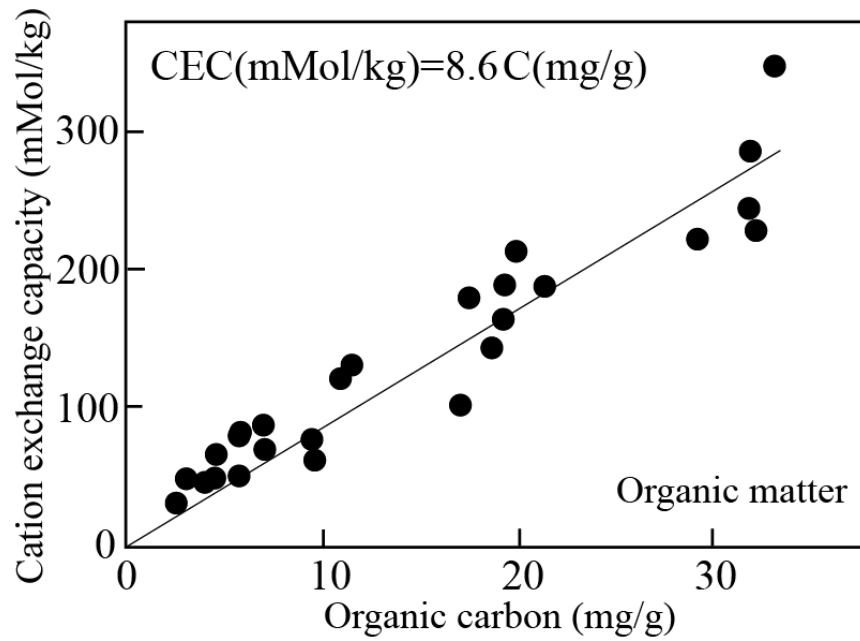
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875 **Figure 4.** Surface sites of organic substances such as humic acids. **a.** The surface of organic  
 876 matter is generally negative at neutral pH values and is characterized by very high values of  
 877 specific surface area and cation exchange capacity. Surface charge can be positive below pH  
 878 2. In addition to a pH-dependent charge on the surface of these macromolecules, there is a  
 879 permanent electric charge associated with isomorphous substitutions. **b.** Example of humic  
 880 acid (Leonardite) showing different types of surface sites. Note that CEC also increases with  
 881 oxidation of such organic molecules (modified from  
 882 [http://www.phelpstek.com/portfolio/samples/humic\\_acid.html](http://www.phelpstek.com/portfolio/samples/humic_acid.html)).

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**Figure 5.** Correlation between cation exchange capacity (CEC) of organic matter and amount of organic carbon (weight concentration, experimental data from Liang et al., 2006).

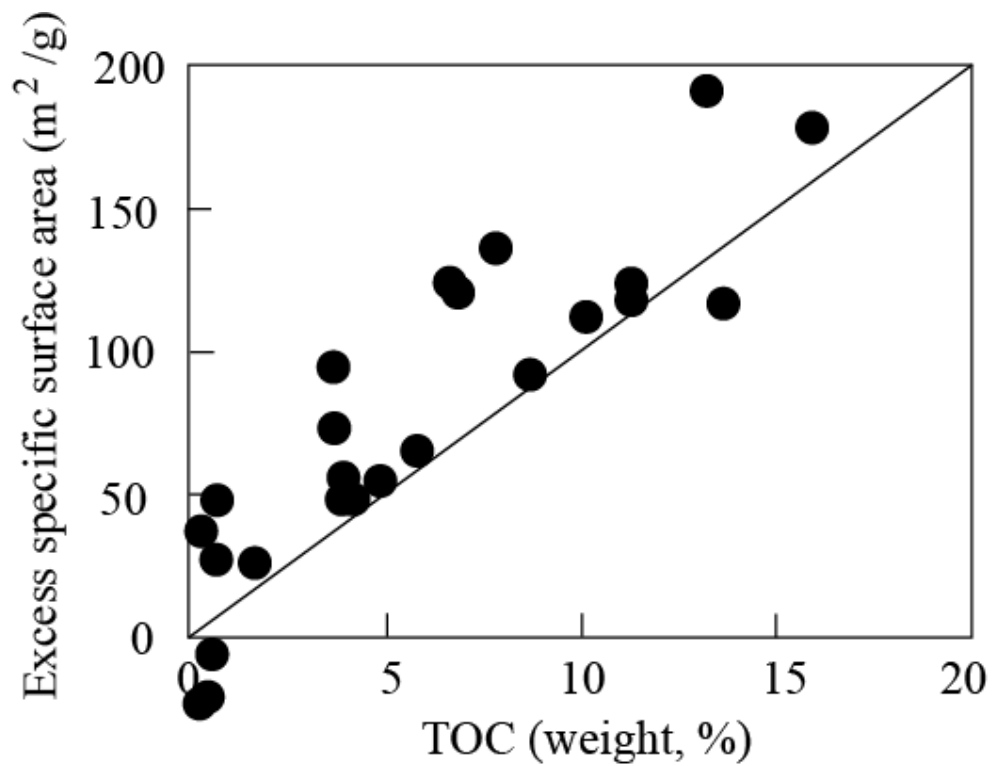
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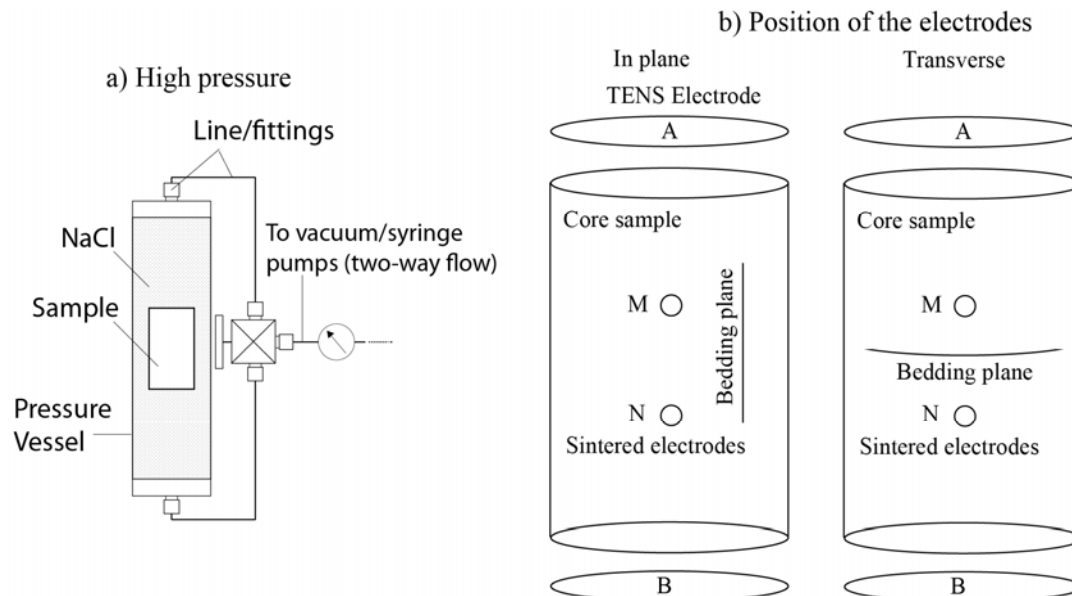
897 **Figure 6.** Relationship between excess specific surface area (clay contribution removed) and  
898 total organic content (weight%) for kerogen-rich oil shales. Data from Derkowski and  
899 Bristow (2012) for the Woodford formation.

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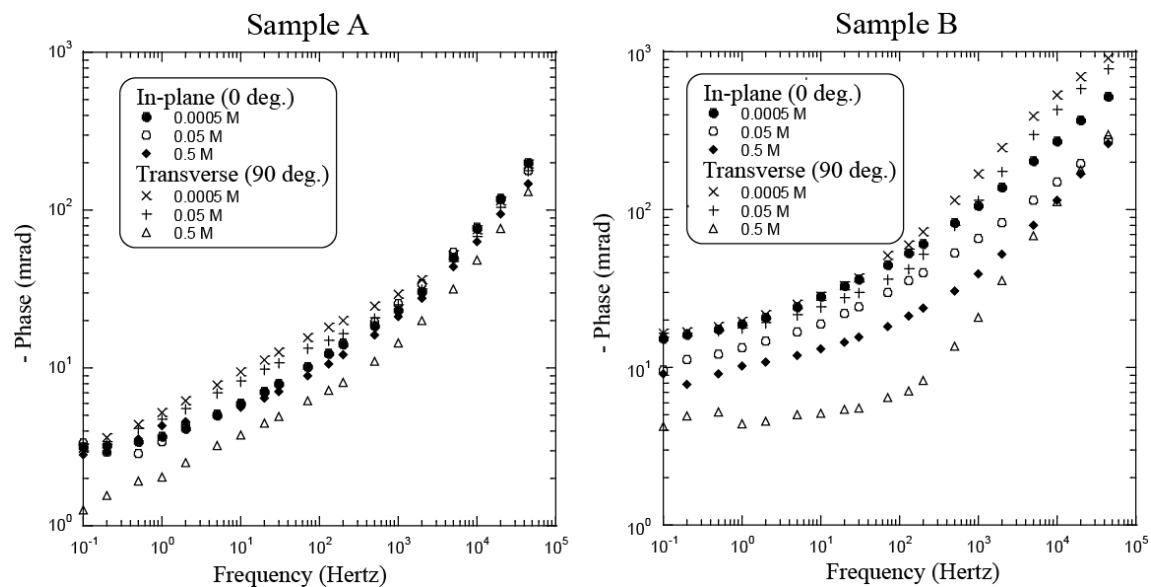
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907 **Figure 7.** Cell and geometry of measurement acquisition for transverse and in-plane electrical  
 908 conductivity measurements with respect to bedding plane. **a.** Sketch of the cell. **b.** Geometry  
 909 of the electrodes. A and B denote current electrodes while M and N denote voltage  
 910 electrodes. The geometric factor was computed as  $k = A/L$ , where  $L$  is the distance between  
 911 the M and N electrodes (1/3 of the height of the sample) and  $A$  is the cross sectional area of  
 912 the cylindrical core sample. The current electrodes are coupled to the sample with a  
 913 conductive electrolytic gel-adhesive (designed for use on human skin in nerve stimulation  
 914 therapy applications), while the potential electrodes are coupled to the sample through a  
 915 conductive electrolyte gel. The current electrodes can be removed and reused in repeat  
 916 acquisitions ; here depicted as detached from the sample to illustrate the size and shape,  
 917 corresponding to the end faces of the sample. The sample surface (except at the position of the  
 918 electrodes) is covered with quick dry nail polish, which prevents desaturation and is a good  
 919 insulator.

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925 **Figure 8.** Measured phases for Samples A and B. Note the continuous increase of the  
 926 magnitude of the phase with the frequency. The high frequency response is likely due to  
 927 Maxwell Wagner polarization.

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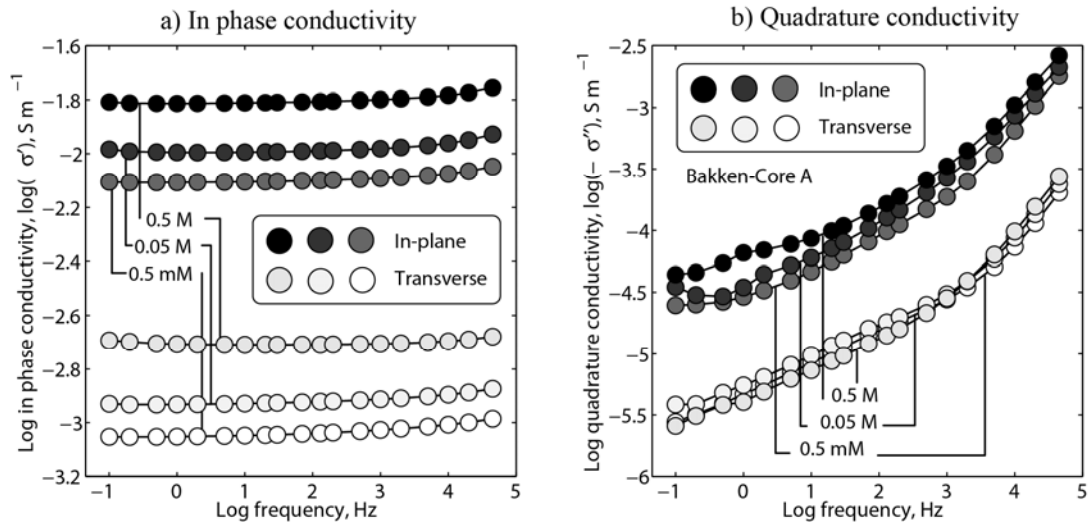
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937 **Figure 9.** Complex conductivity spectra for Bakken core Sample A. **a.** In-phase electrical  
 938 conductivity versus frequency at three salinities (0.5, 0.05, and 0.005 M NaCl). **b.** quadrature  
 939 electrical conductivity versus frequency at three salinities (0.5, 0.05, and 0.005 M NaCl).

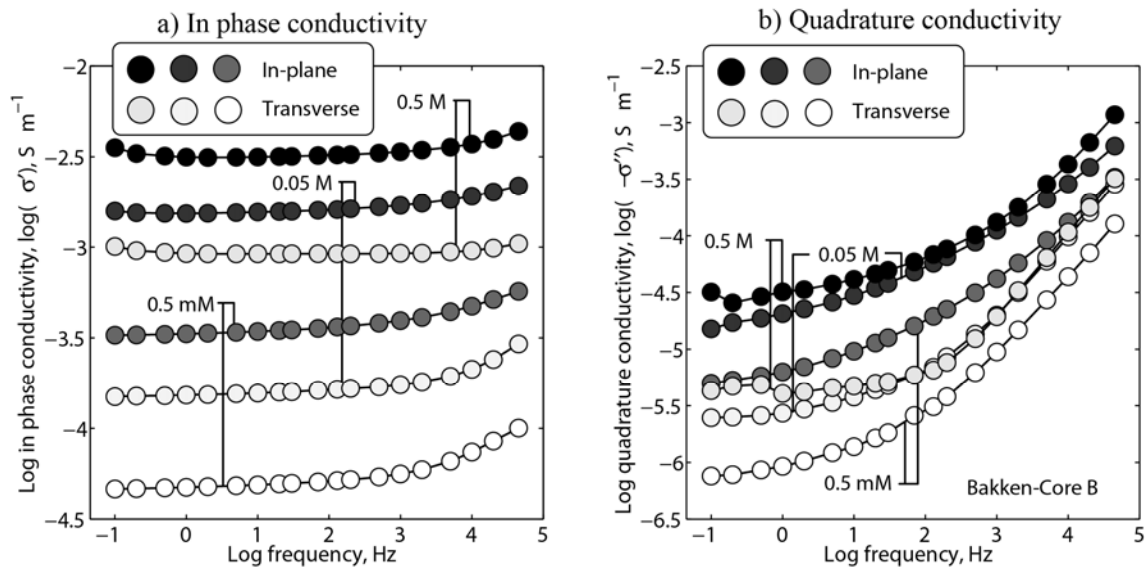
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947 **Figure 10.** Complex electrical conductivity spectra of Bakken core Sample B. **a.** In-phase  
 948 electrical conductivity versus frequency at three salinities (0.5, 0.05, and 0.005 M NaCl). **b.**  
 949 quadrature electrical conductivity versus frequency at three salinities (0.5, 0.05, and 0.005 M  
 950 NaCl).

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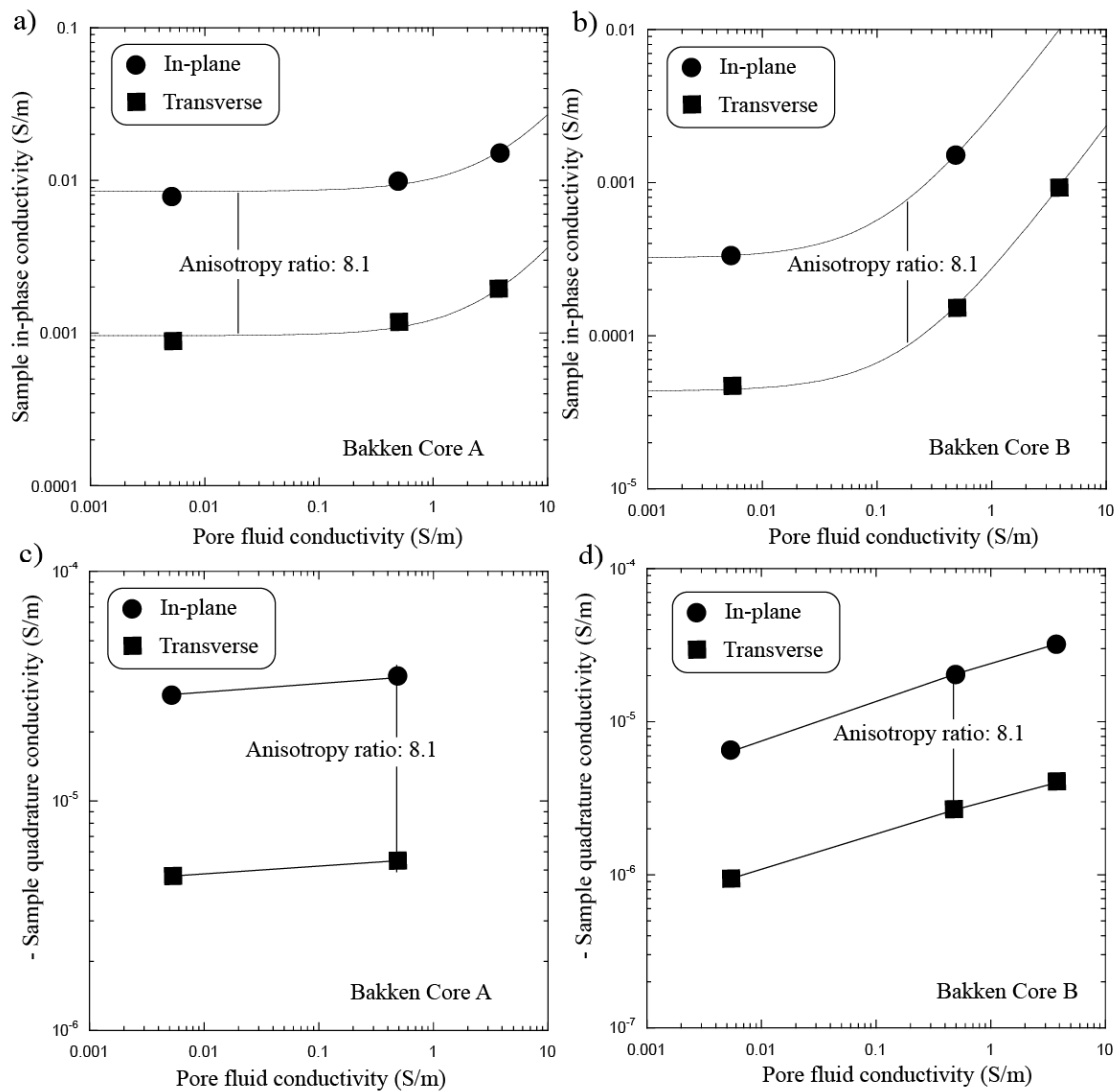
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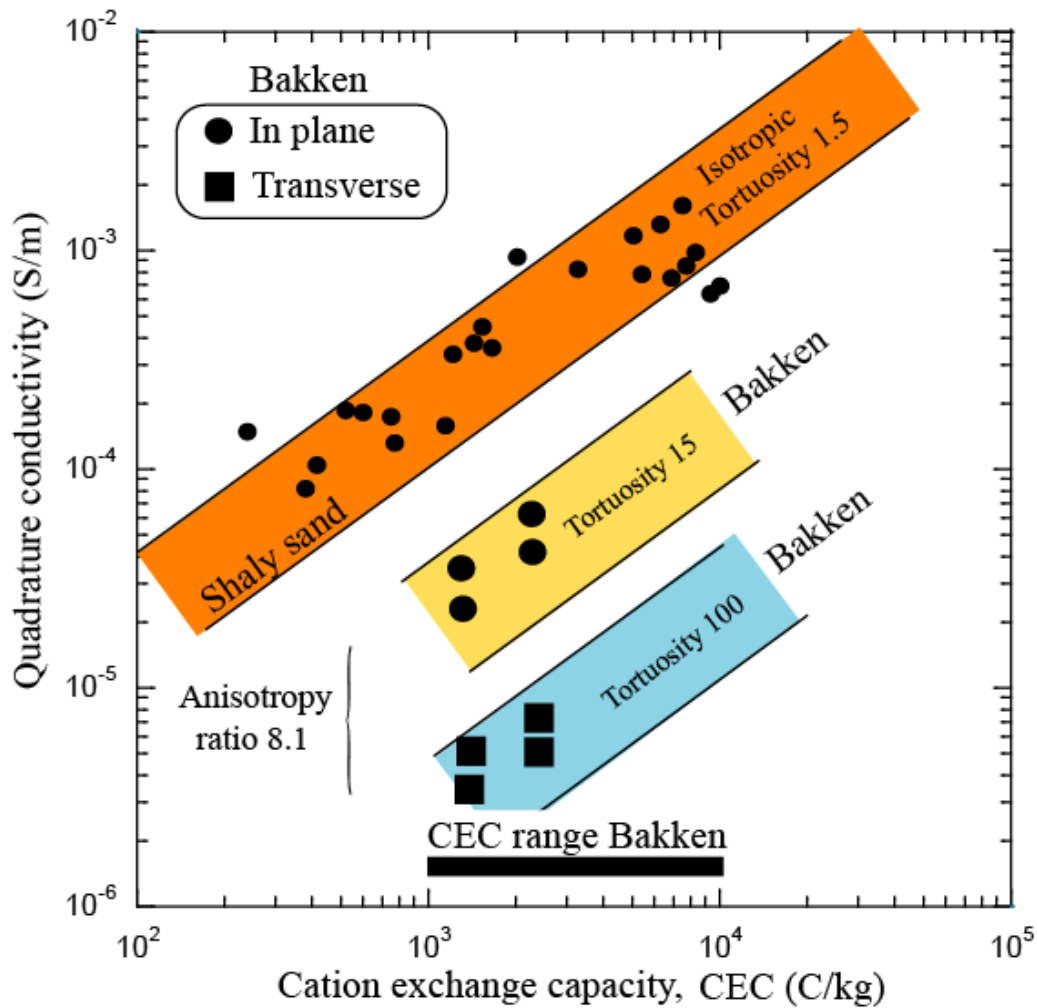


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957 **Figure 11.** In-phase and quadrature electrical conductivities for core samples A and B at 1  
 958 Hertz. **a.** In-phase electrical conductivity, Sample A. Lines identify the model fit (equation 5  
 959 at saturation). **b.** In-phase conductivity, Sample B. For the two upper graphs, the lines  
 960 identify the model fit. Formation factors and surface conductivities are reported in Table 3. **c.**  
 961 Quadrature electrical conductivity, Sample A (the points at the highest salinity are not shown  
 962 because of their uncertainties). The vertical line serves as guide. **d.** Quadrature conductivity,  
 963 Sample B. For the two lower graphs, the lines serve as guides. Anisotropy ratio is defined as  
 964 the ratio of the highest to the lowest eigenvalues of the tensor; it exhibits a mean of  $8.1 \pm 3.1$   
 965 ( $N = 12$ ).

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970 **Figure 12.** Influence of anisotropy and tortuosity upon quadrature conductivity (1 Hertz).

971 The high tortuosities found in Bakken rocks are responsible for a decrease of quadrature

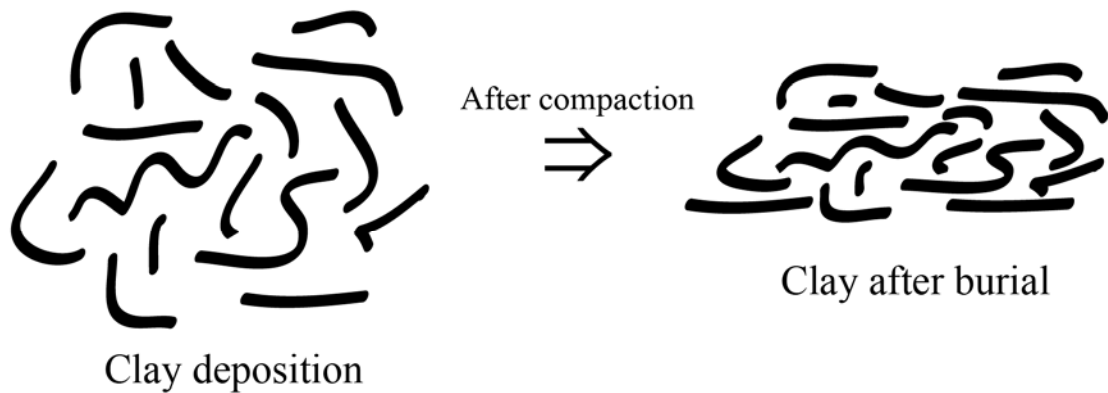
972 conductivity at a given salinity and CEC. For Bakken rock samples, data are consistent with a

973 tortuosity value of 15 in the bedding plane and over 100 in the transverse direction.

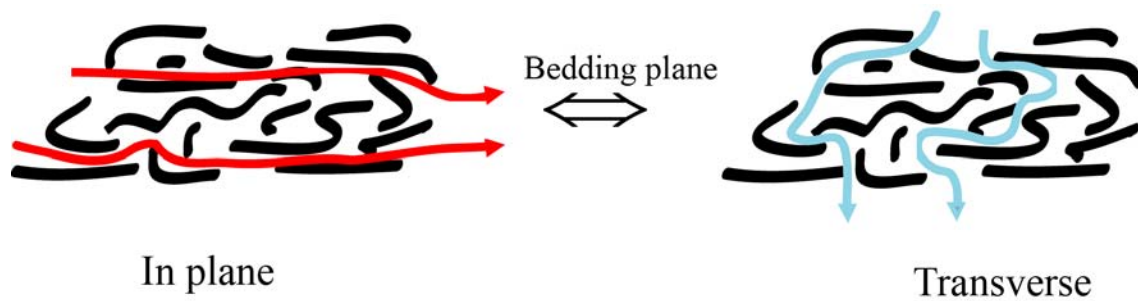
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## a) Influence of compaction on the petrofabric



## b) Impact on the tortuosity



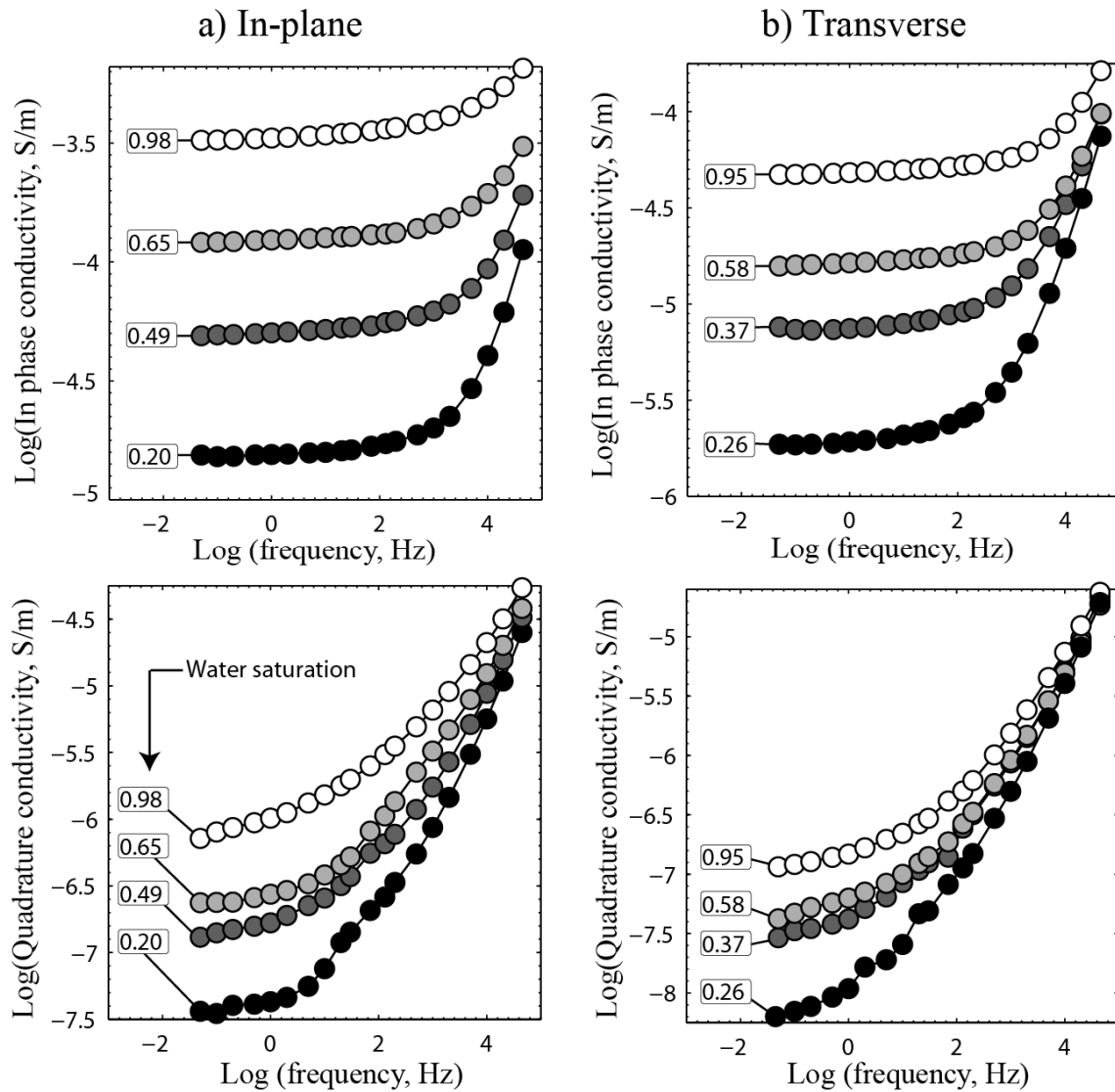
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978 **Figure 13.** Influence of burial on both petrofabric and tortuosity tensor. **a.** Differential  
 979 compaction is responsible for the formation of petrofabric in clayey materials (clay particles  
 980 are shown in black). Depositional facies and burial are typically responsible for the formation  
 981 of TI (transversely isotropic) media. **b.** In TI media, the in-plane tortuosity is expected to be  
 982 much smaller than the tortuosity in the direction transverse to bedding plane.

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987 **Figure 14.** Influence of saturation upon in phase and quadrature conductivities of Sample B.988 **a.** In-plane measurements for in-phase and quadrature conductivities. **b.** Transverse

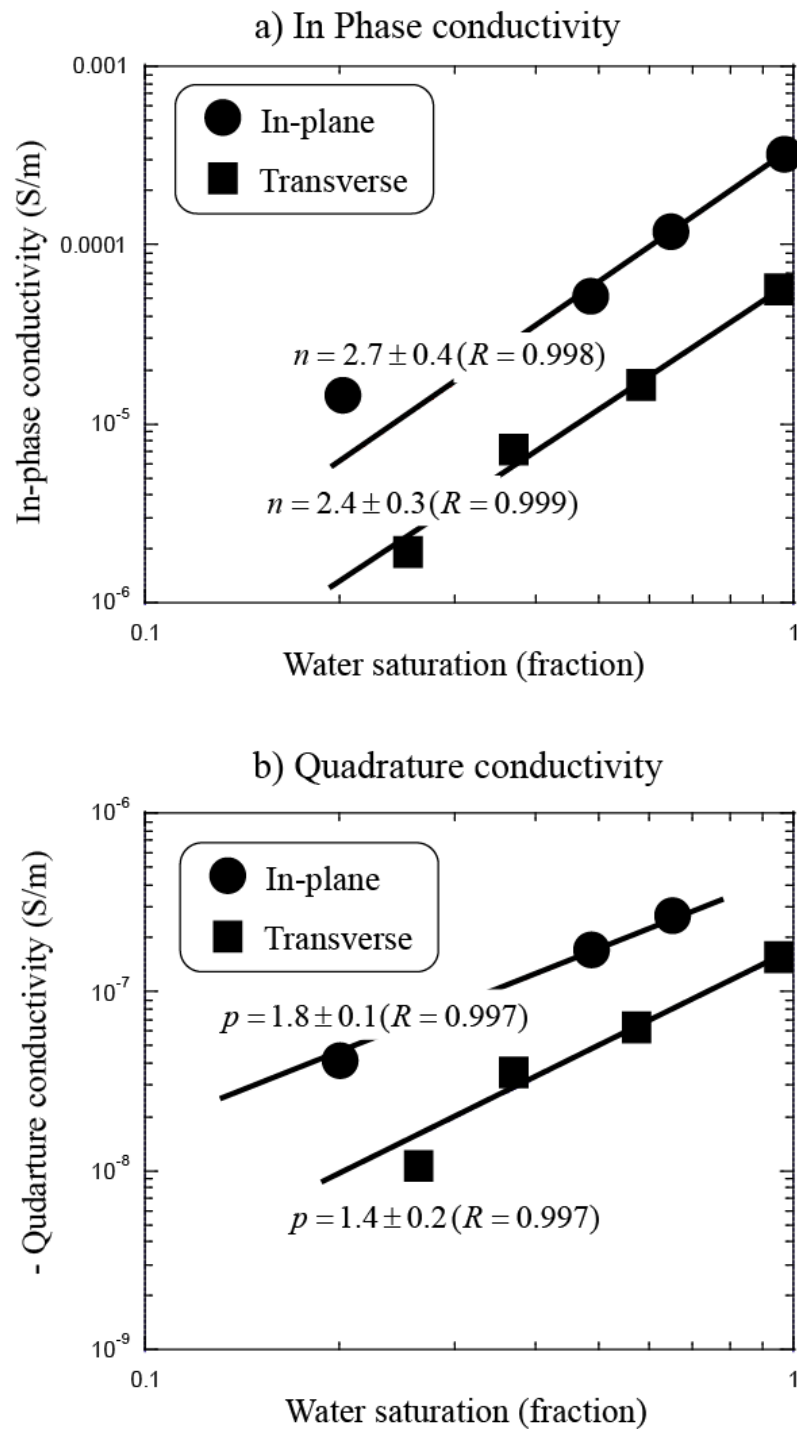
989 measurements for in-phase and quadrature conductivities. Note that a change in saturation

990 affects the magnitude of the in-phase and quadrature conductivities, not the anisotropy ratio.

991 This result is consistent with our assumption to consider that  $n$  and  $p$  do not depend too much

992 on the direction.

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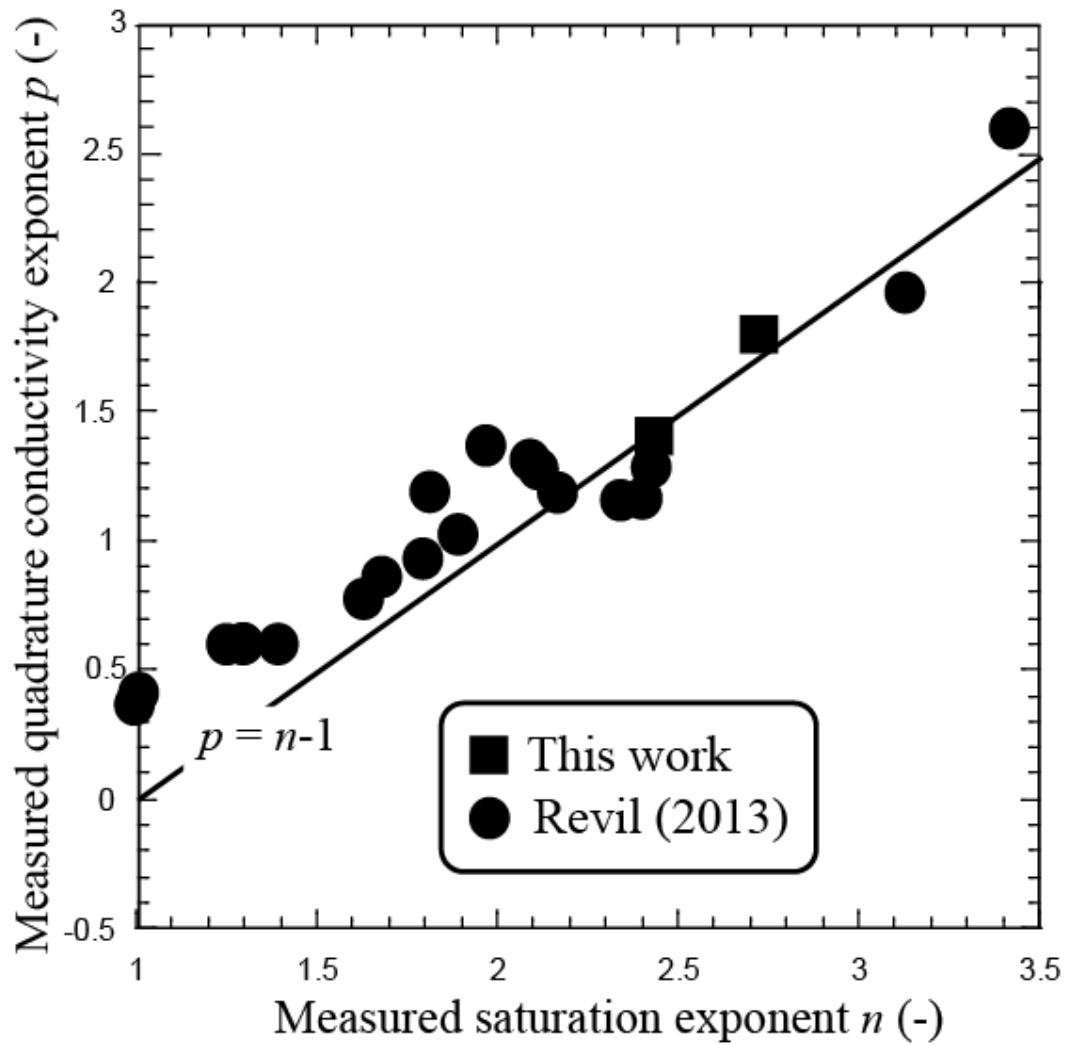
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996 **Figure 15.** Influence of the saturation on the in-phase and quadrature conductivity of Sample  
 997 B at 1 Hz. **a.** In-phase conductivities (in-plane and transverse measurements). **b.** Quadrature  
 998 conductivities (in-plane and transverse measurements).

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1003 **Figure 16.** Relationship between the  $p$ -exponent used to describe the saturation dependence  
 1004 of the quadrature conductivity and the  $n$ -exponent (saturation exponent) used to describe the  
 1005 saturation dependence of the in-phase conductivity when surface conductivity is negligible.  
 1006 The plain line corresponds to the relationship developed in Revil (2013), which is consistent  
 1007 with the prediction of the model of Vinegar and Waxman (1984).

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